



Connecting Band Structure to Sub-picosecond Spectral Photoemission Properties

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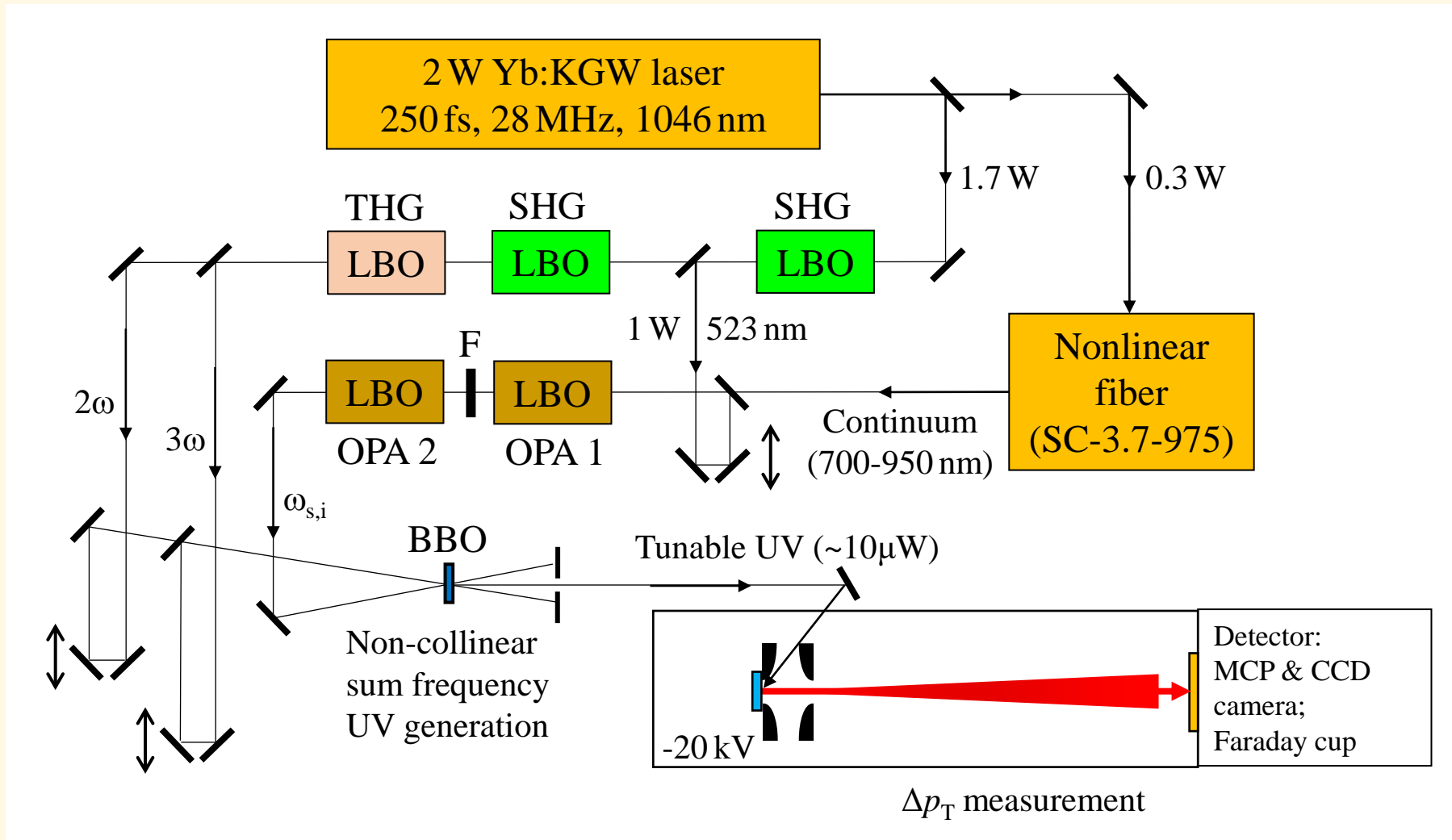
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- GaSb(001)
 - Excited-state thermionic emission (ESTE)
- Cu(111)
 - Sub-threshold (non-surface-state) emission from upper conduction band
- Hf(0001)
 - ‘Sub-Dowell-Schmerge’ spectral *MTE* dependence due to low m^* emission band
- Additional theoretical considerations for (quasi-)instantaneous photoemission
 - Heisenberg Uncertainty
 - Group velocity

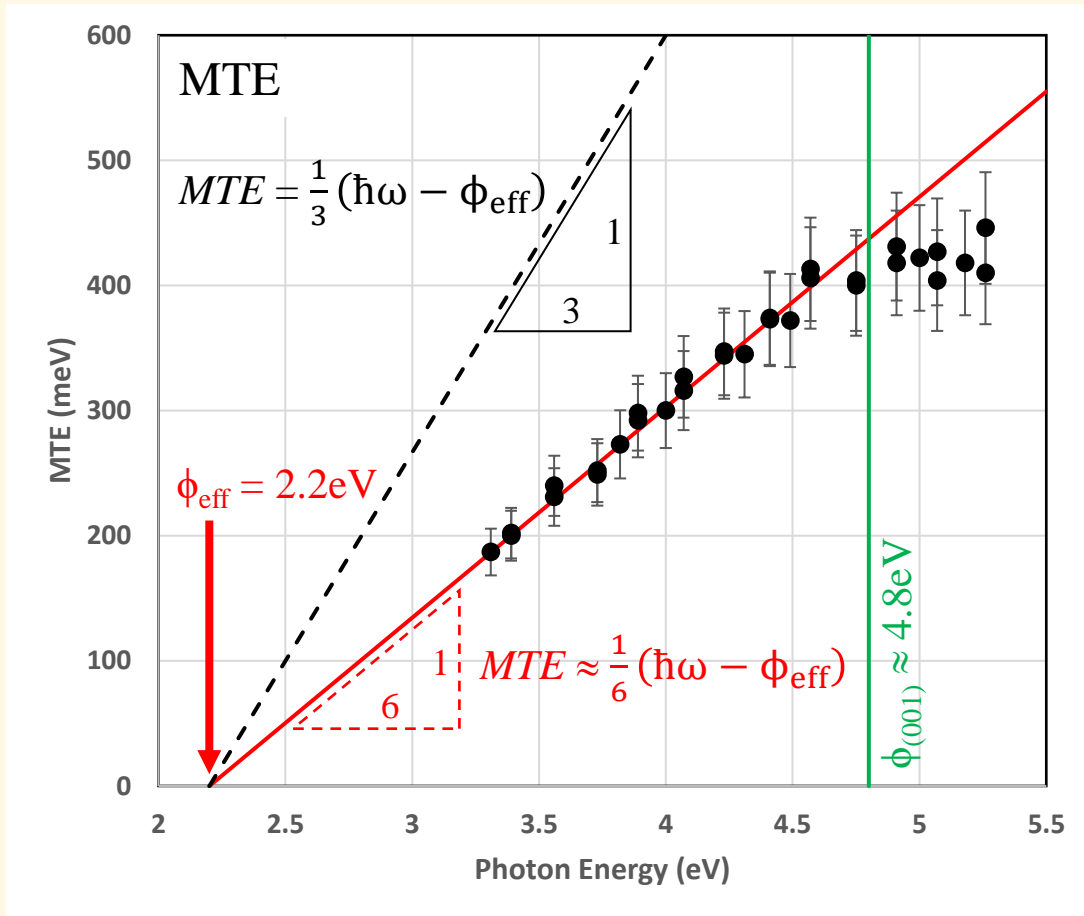
Tunable UV radiation source

– Laser / NLO based radiation source: 3.0 – 5.3eV (235-410nm)



GaSb(001): MTE measurements

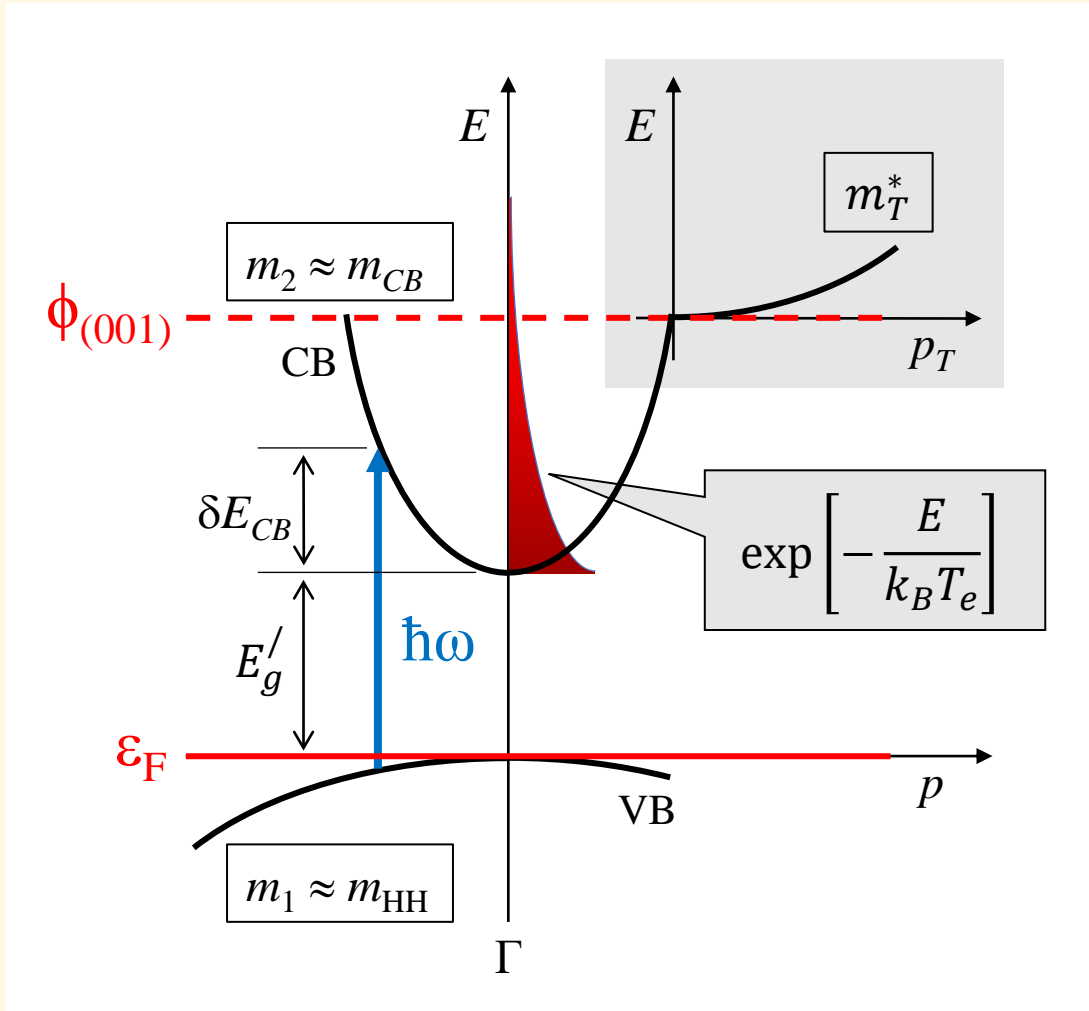
– Photoemission data using UV-tunable (235-410nm) sub-picosecond (~ 0.5 ps) laser pulses; GaSb(001) wafer



- Sub-threshold ($\hbar\omega < \phi_{(001)}$) photoemission with $\phi_{\text{eff}} = 2.2\text{eV}$
- ‘Sub-Dowell-Schmerge’ spectral *MTE* dependence \Rightarrow Excited state thermionic emission (ESTE)
 - ... Boltzmann tail emission (above vacuum level) from hot thermalized electron distribution photoexcited into upper conduction band with a low effective mass m^*
- Additional contribution from direct one-step photoemission for $\hbar\omega > \phi_{(001)}$

GaSb(001): ESTE

– Parabolic band approximation



- Photoemission analyses for Boltzmann tail emission:

$$MTE \geq \left| \frac{m_T^*}{m_0} \right| k_B T_e ; \left| \frac{m_T^*}{m_0} \right| \rightarrow 1 \text{ for } m_T^* \geq m_0$$

... **no** recipient vacuum density of states

- Thermalized initial photoexcited electron temperature:

$$\frac{3}{2} k_B T_e = \delta E_{CB} = \frac{m_1}{m_1 + m_2} (\hbar\omega - E_g')$$

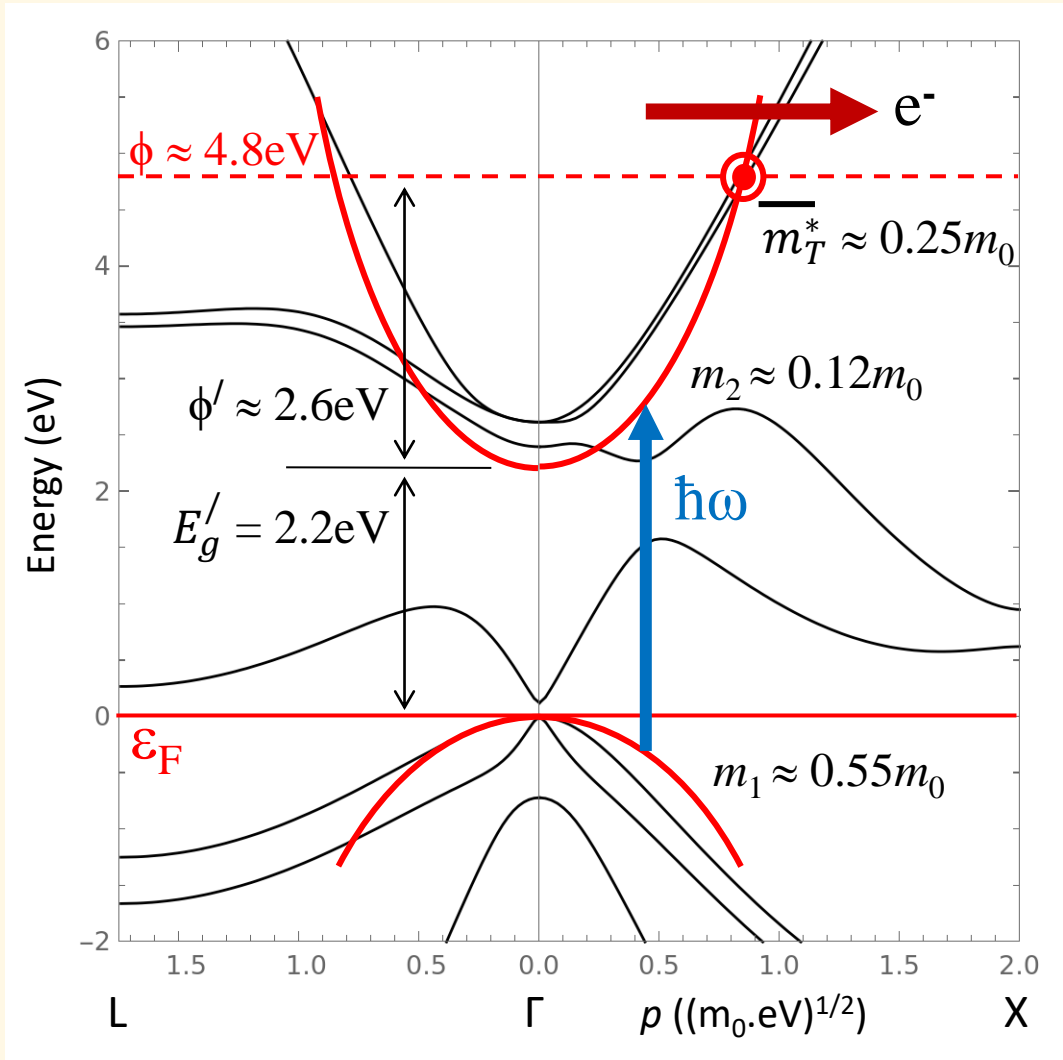
$$\therefore MTE \geq \frac{2}{3} \left| \frac{m_T^*}{m_0} \right| \frac{m_1}{m_1 + m_2} (\hbar\omega - E_g')$$

THUS:

$$E_g' = \phi_{\text{eff}} = 2.2\text{eV} \text{ and } \left| \frac{m_T^*}{m_0} \right| \frac{m_1}{m_1 + m_2} \approx \frac{1}{4} \quad ??$$

GaSb: Band structure

– Full relativistic calculation with spin-orbit coupling; PAW & PBE functional; **No** ‘scissor’ operator



- Energy gap inconsistencies:

$E_g'(\text{expt.}) = 2.2\text{eV}$	$E_g'(\text{DFT}) = 2.6\text{eV}$
$E_g(\text{meas.}) = 0.67\text{eV}$	$E_g(\text{DFT}) = 0.16\text{eV}$
300K	0K

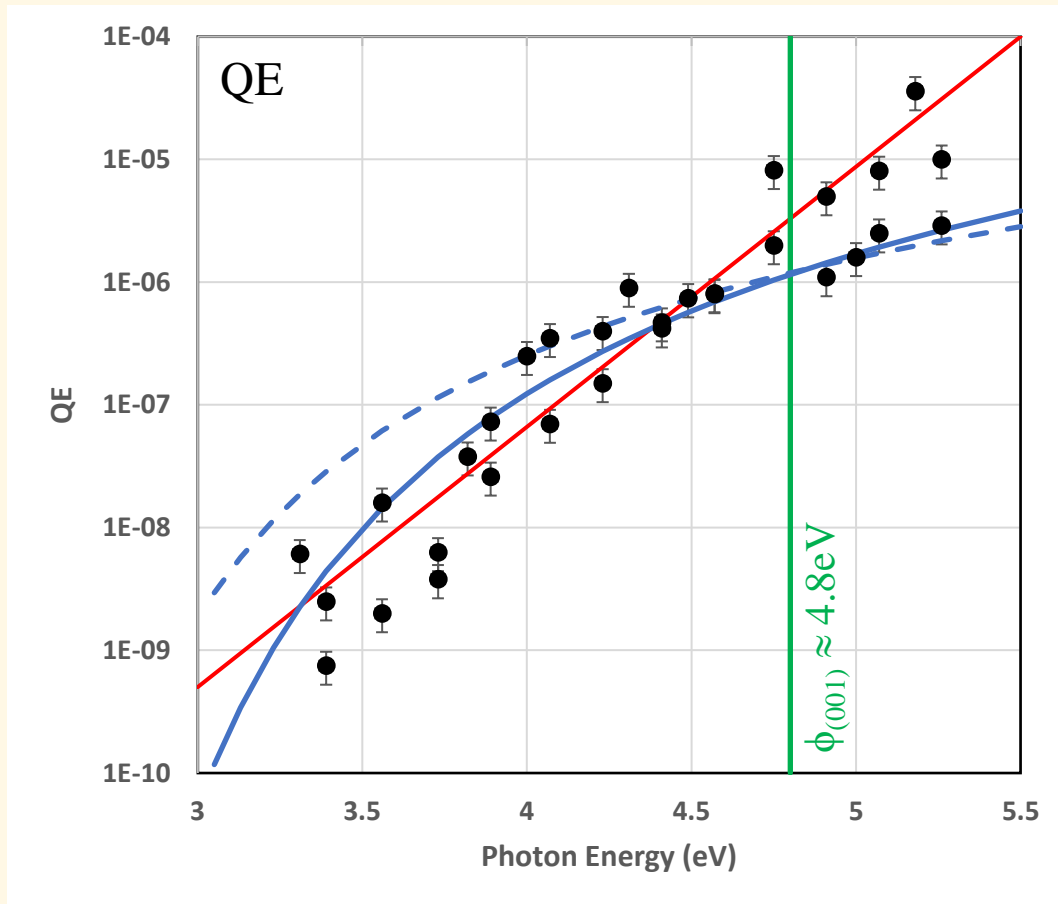
- Effective masses and predicted *MTE*:

$$\left| \frac{m_T^*}{m_0} \right| \frac{m_1}{m_1+m_2} \approx 0.21$$

$$\therefore MTE \geq \frac{2}{3} \left| \frac{m_T^*}{m_0} \right| \frac{m_1}{m_1+m_2} (\hbar\omega - E_g') \approx 0.14 (\hbar\omega - E_g')$$

... parabolic band approximation
c.f. $MTE_{\text{expt.}} \approx \frac{1}{6} (\hbar\omega - E_g')$

GaSb(001): Quantum efficiency



- For $\hbar\omega \leq \phi_{(001)}$, QE increases by 1,000 \times as photon energy increases by 1.5eV
 - T_e increases from 7,200K to 17,000K
- $QE(\hbar\omega)$ difficult to explain by standard thermionic emission
 - $\phi = 4.8\text{eV}$ (—) and $\phi = 2.6\text{eV}$ (---)

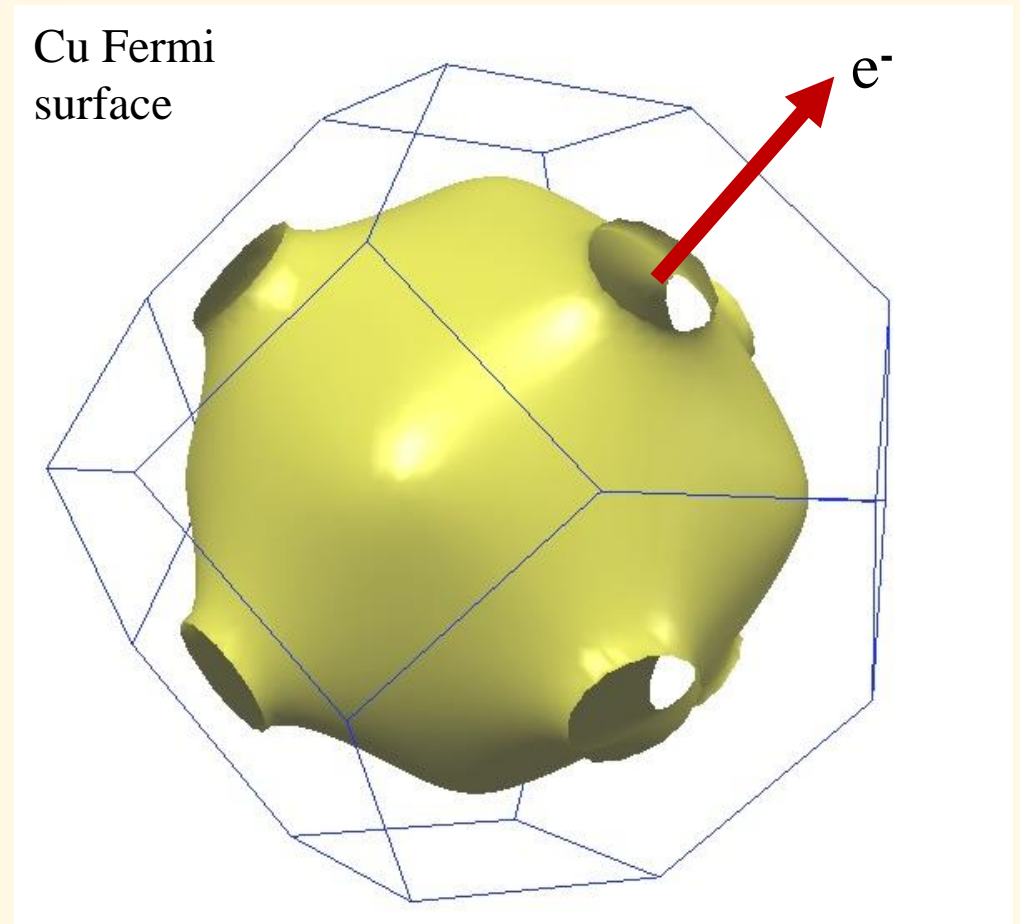
$$QE = A (k_B T_e)^2 \exp\left[-\frac{\phi}{k_B T_e}\right]$$

$$\dots \text{ with } k_B T_e = \frac{2}{3} \left(\frac{m_1}{m_1 + m_2}\right) (\hbar\omega - E_g')$$

- Bulk emission band $E(\mathbf{p})$ and DOS need to be included, as well as vacuum DOS
- Improved QE measurements also required
 - More stable tunable UV laser radiation source currently in development

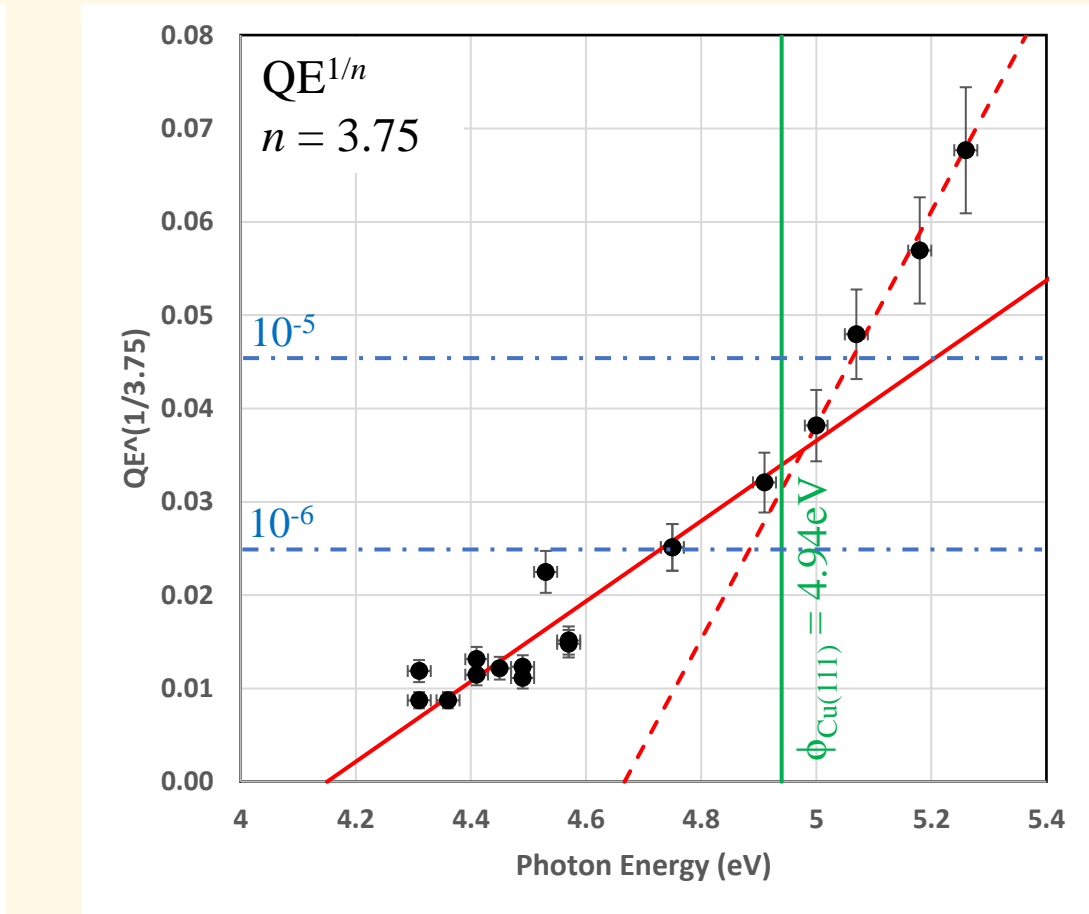
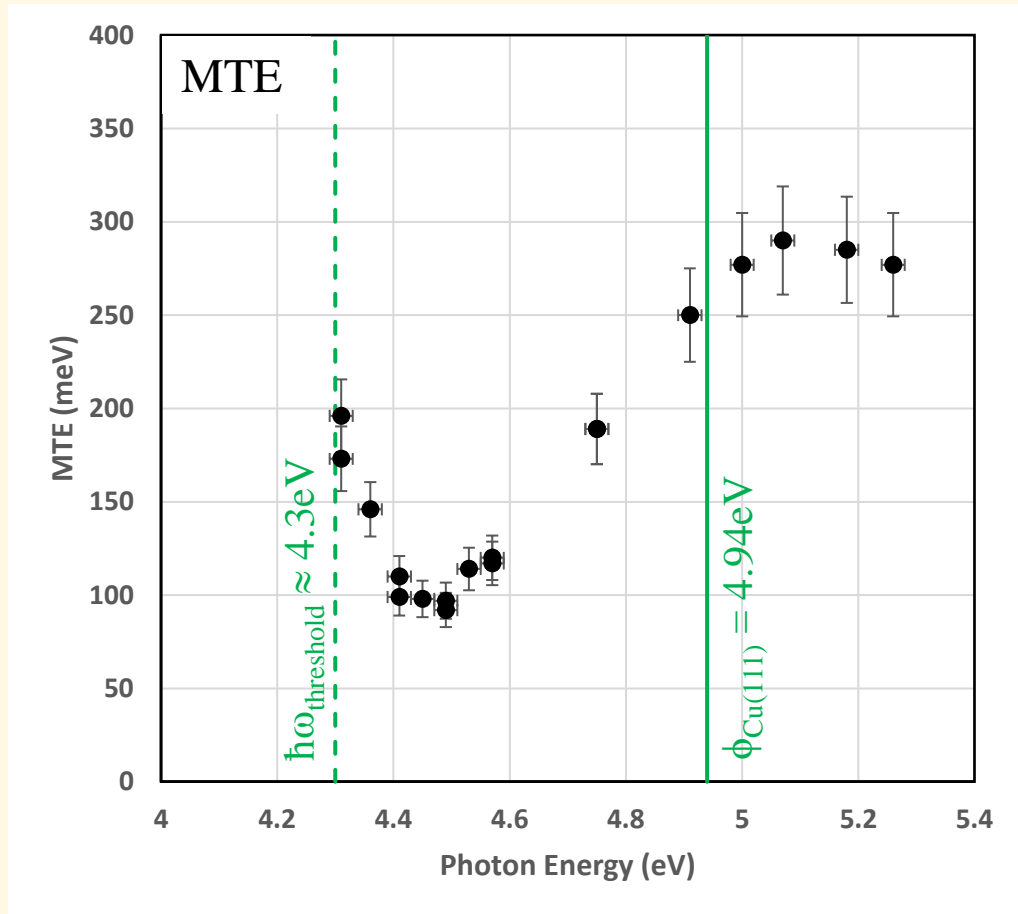
Cu(111) photocathode

- Work function: $\phi_{\text{Cu}(111)} = 4.94\text{eV}$
- Photocathode properties:
 - Polished: Surface roughness $< 10\text{nm rms}$ (**not** atomically flat)
 - Surface **not** clean ($\Delta\phi_{\text{-O-Cu}} \approx -0.4\text{-}0.5\text{eV}$)
 - \Rightarrow **No** surface states AND $\phi_{\text{eff.}} \approx 4.5\text{eV}$
- Fermi surface ‘hole’ in $\Gamma \rightarrow \text{L}$ direction
 - \Rightarrow Extra $\geq 0.2\text{eV}$ transverse energy required for photoemission from occupied bands
 - \therefore Expect $\phi_{\text{emission}} \geq 4.7\text{eV}$



Cu(111): Sub-threshold photoemission

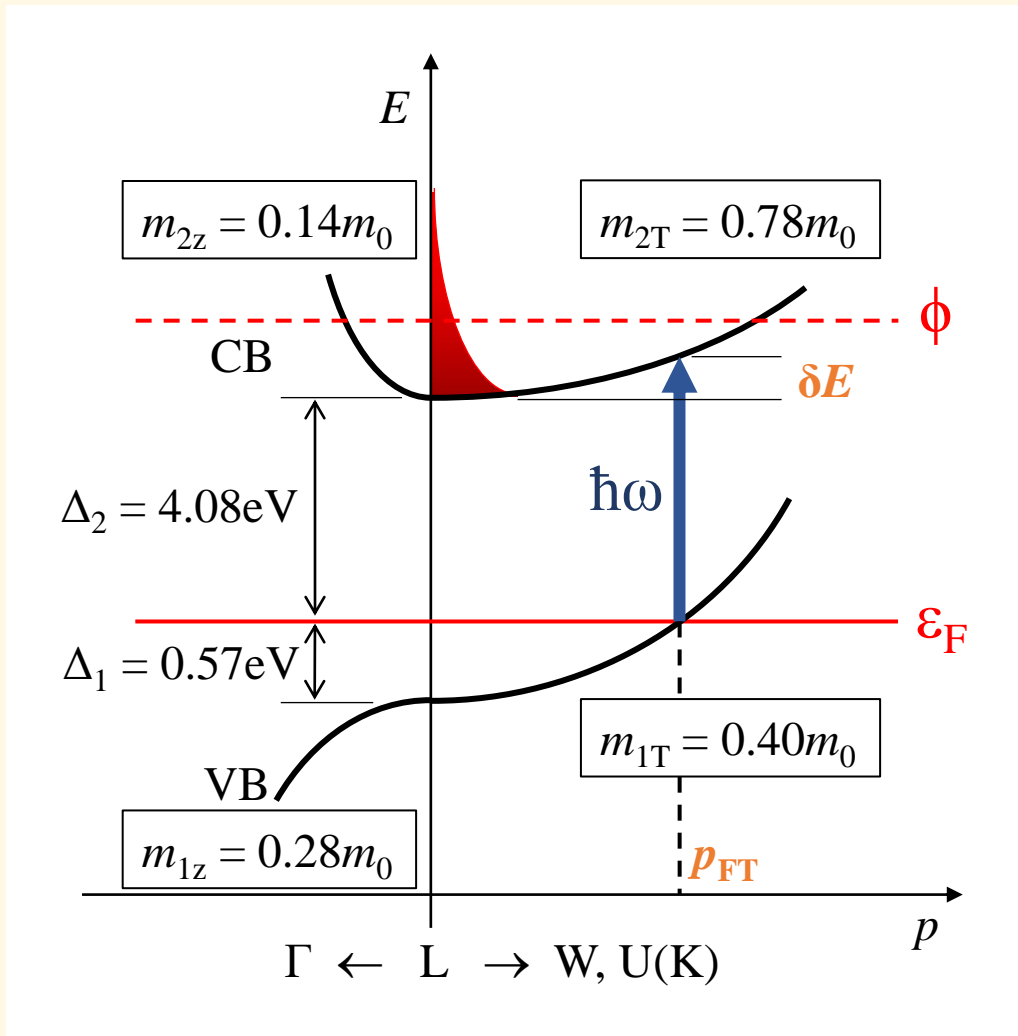
– Photoemission data using UV-tunable (235-410nm) sub-picosecond (~ 0.5 ps) laser pulses



... An ultrafast / band structure effect

Cu(111): Emission mechanism

– L-point band structure; Parabolic approximation



Emission of the Boltzmann tail (above the vacuum level) of a hot thermalized photo-excited electron distribution:

- At ‘threshold’: $\hbar\omega \approx 4.3\text{eV}$

$$\Rightarrow \delta E = \frac{p_{FT}^2}{2m_{2T}} = \frac{m_{1T}\Delta_1}{m_{2T}} \approx 0.29\text{eV}$$

$$\therefore MTE \geq \left| \frac{m_{2T}}{m_0} \right| k_B T_e = \frac{2}{3} \left| \frac{m_{2T}}{m_0} \right| \delta E \approx 150\text{meV}$$

... **no** vacuum states and surface roughness

LEMMA:

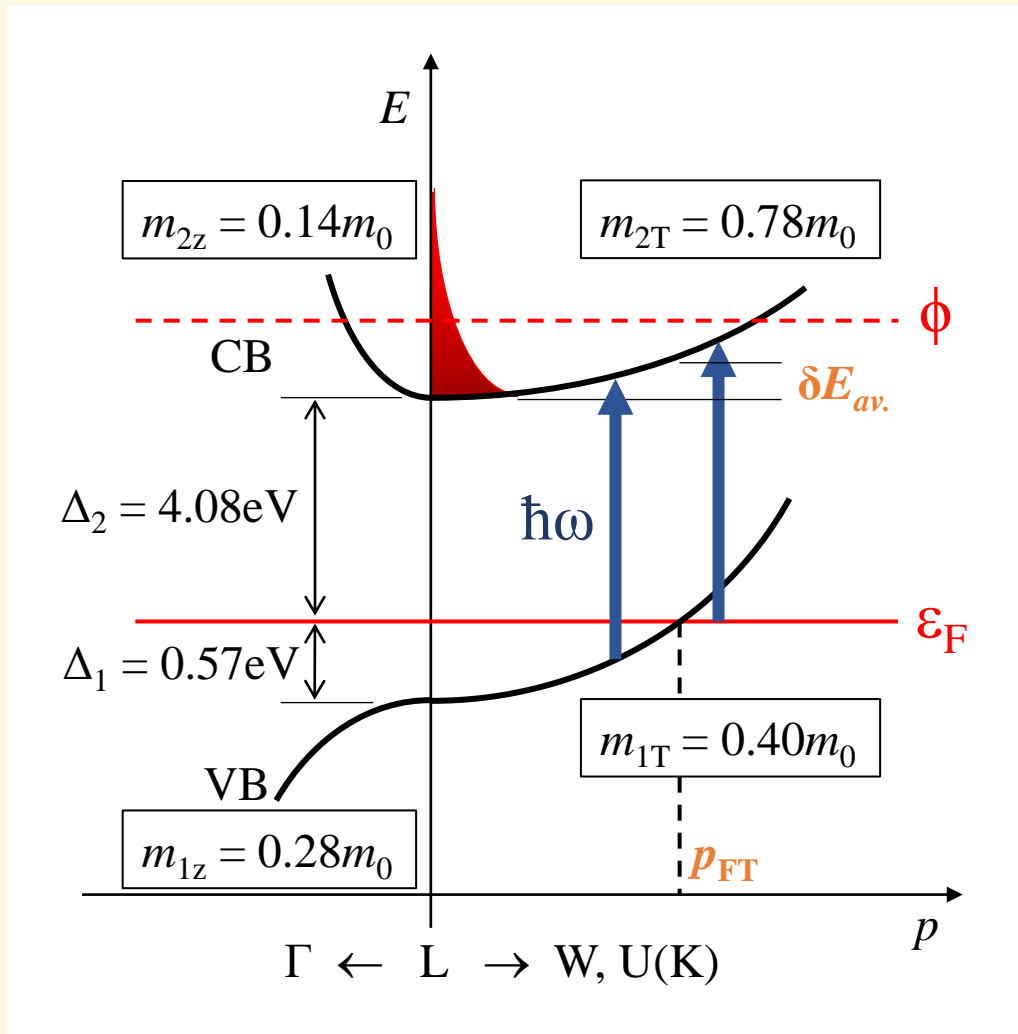
$$\hbar\omega = \Delta_2 + \delta E \approx 4.3\text{eV}$$

$$\Rightarrow \Delta_2 \approx 4.01\text{eV}$$

... close !

Cu(111): Emission mechanism

– L-point band structure; Parabolic approximation



- At $\hbar\omega \approx 4.5\text{eV} < \Delta_1 + \Delta_2 = 4.65\text{eV}$
 - Hot electron photoexcitation limited by Fermi level
 - More lower energy electrons photoexcited

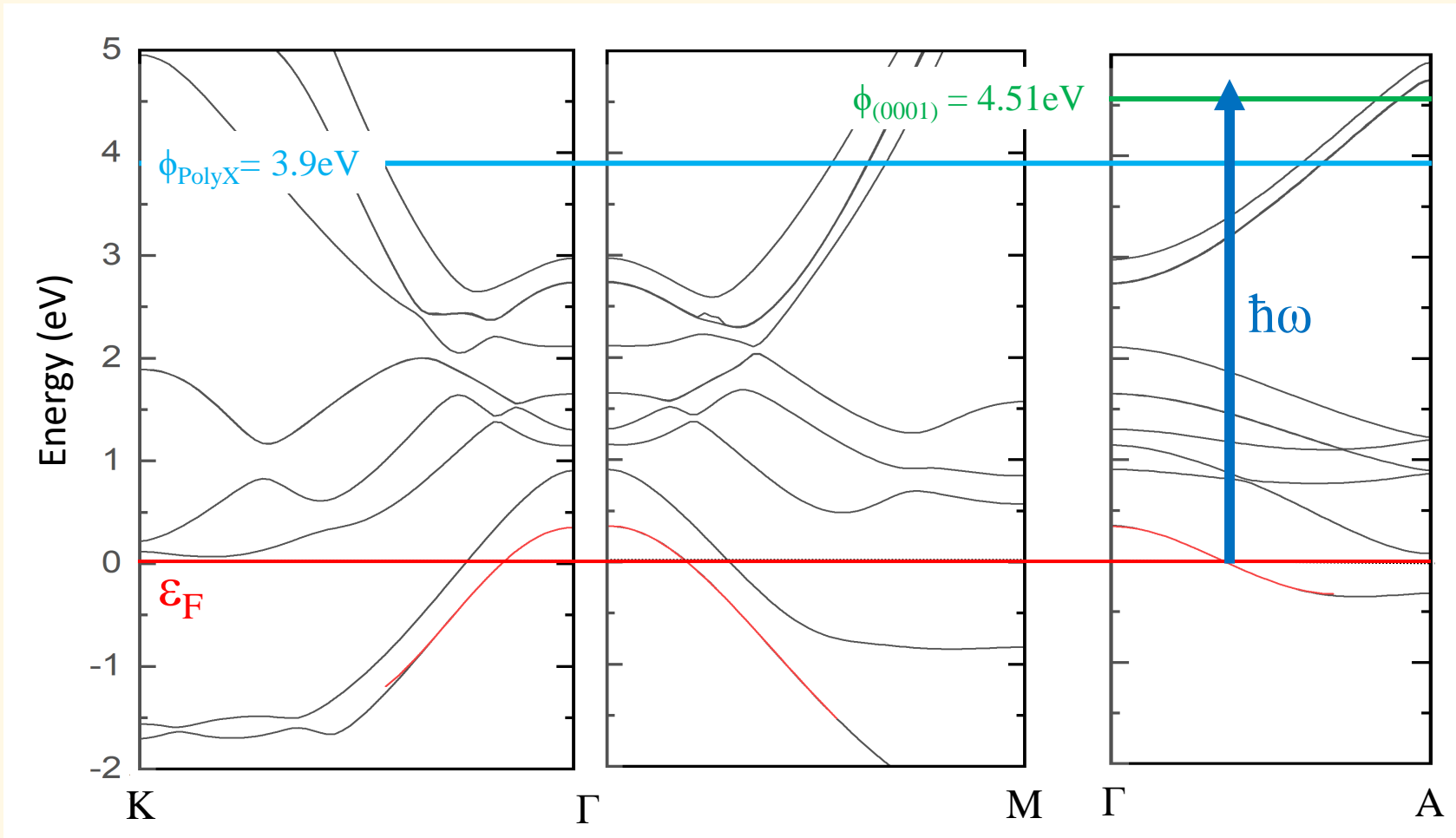
\therefore Expect $\delta E_{av.} \leq 0.2\text{eV}$

$\Rightarrow MTE \geq \frac{2}{3} \left(\frac{m_{2T}}{m_0} \right) \delta E_{av.} \approx 100\text{meV}$
- For $\hbar\omega > \Delta_1 + \Delta_2$
 - $\delta E_{av.}$ increases $\Rightarrow MTE$ increases again
- For $\hbar\omega > \phi - \Delta\phi_{\text{-O-Cu}} + \Delta_1 \approx 5.0\text{eV}$ ($\Rightarrow \Delta\phi_{\text{-O-Cu}} \approx 0.5\text{eV}$)
 - Direct near threshold emission from VB with low MTE

$\therefore MTE$ reduction (**plus QE increase**)

Hf(0001): Band structure

– Full relativistic band structure calculation with spin-orbit coupling



For $\Gamma \rightarrow A$ emission:

- No intermediate upper band states
 \Rightarrow One-step photoemission

- Relatively isotropic *single* hole-like emitting band state

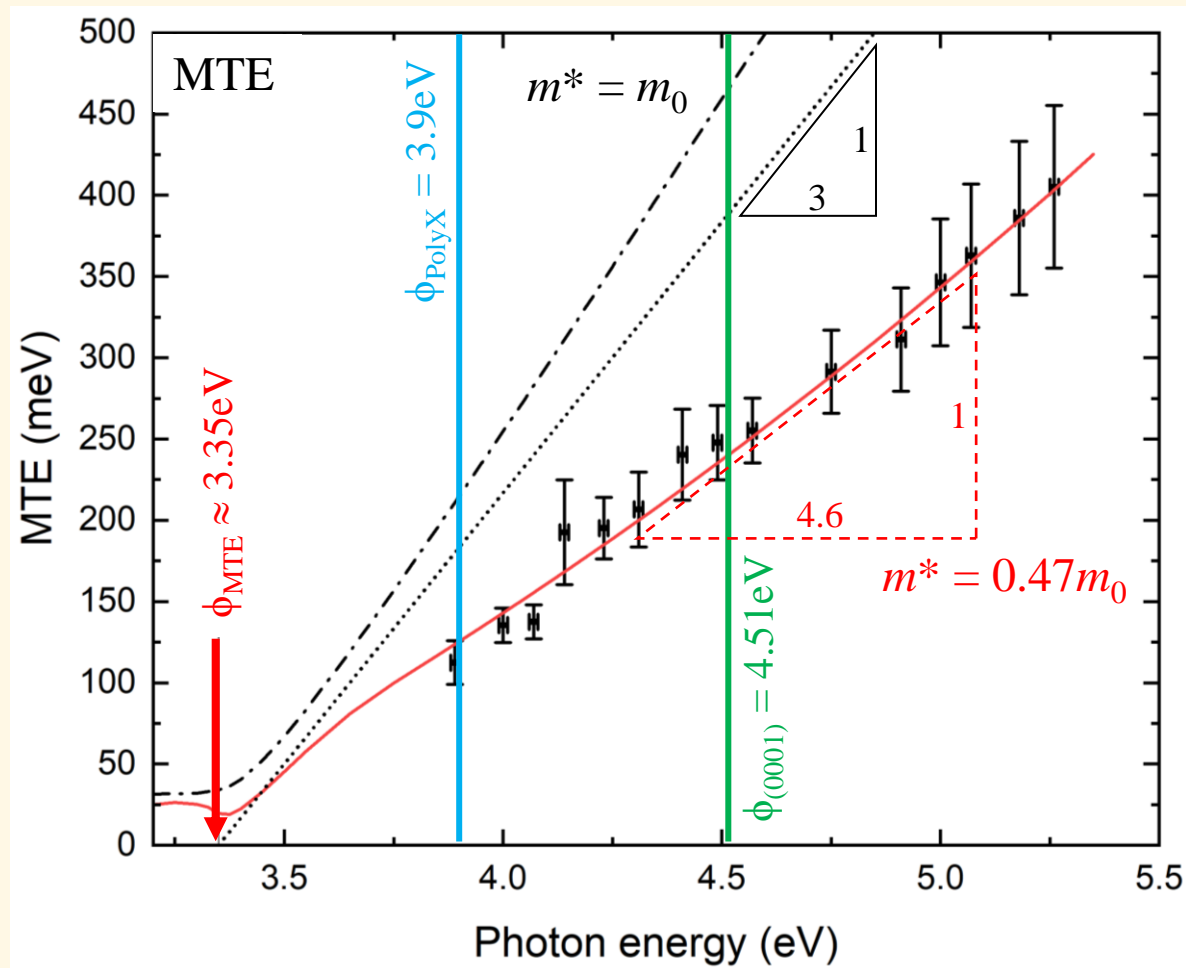
$$m_T^* = m_z = 0.47(\pm 0.02)m_0$$

$$\therefore \text{Expect } MTE < \frac{1}{3}(\hbar\omega - \phi)$$

... dispersion of emitting band state restricts p_T

Hf(0001): MTE measurements

– Photocathode polished to remove HfO₂ layer



- Spectral *MTE* dependence significantly ‘sub-Dowell-Schmerge’ ($m^* = m_0$)

AND consistent with one-step photoemission theory ($m^* = 0.47m_0$)

$$MTE \geq \left| \frac{m_T^*}{m_0} \right| \frac{\hbar\omega - \phi}{3} ; \left| \frac{m_T^*}{m_0} \right| \rightarrow 1 \text{ for } m_T^* \geq m_0$$

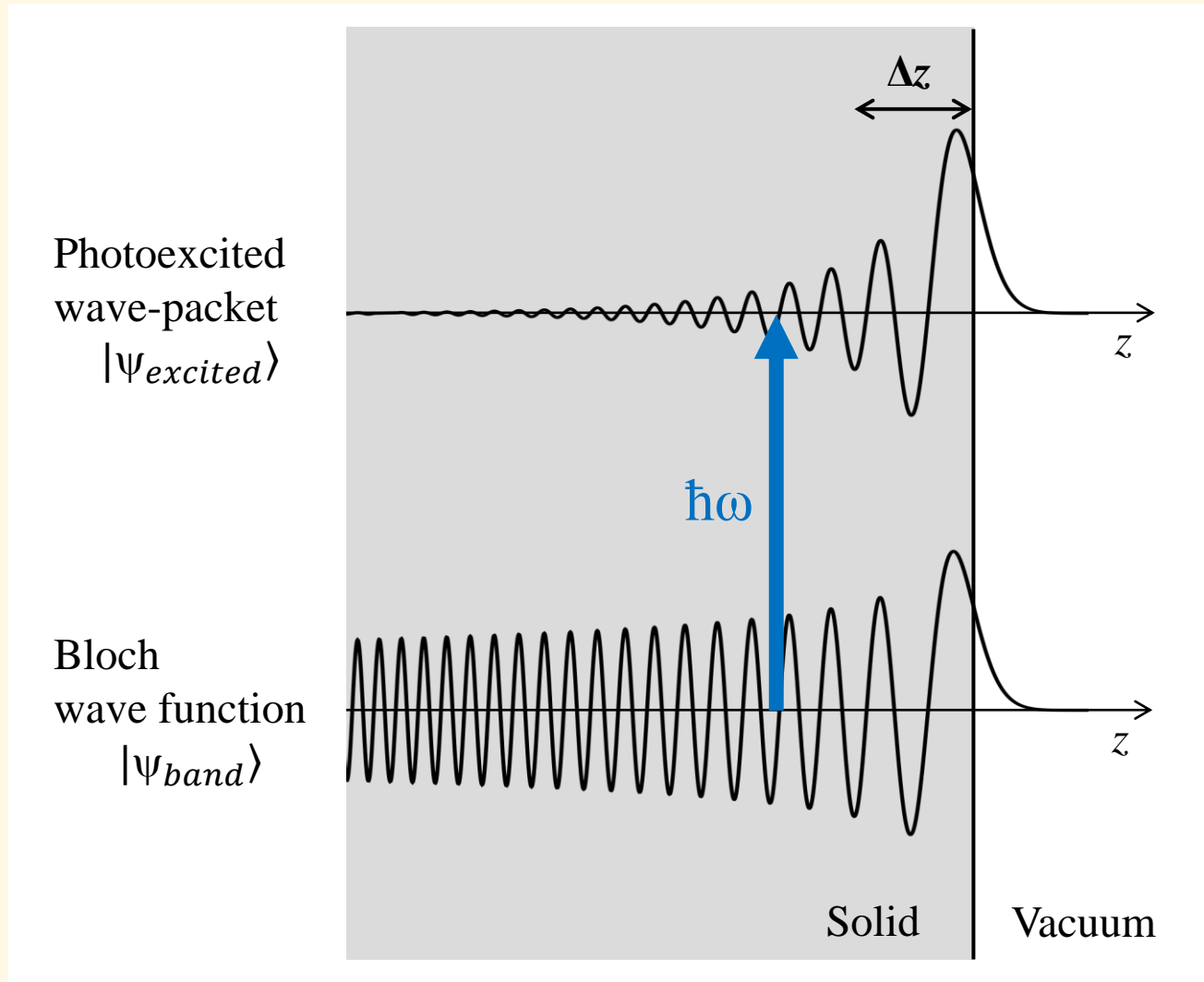
... **no** bulk band or vacuum density of states

BUT

Inconsistencies in work functions ...

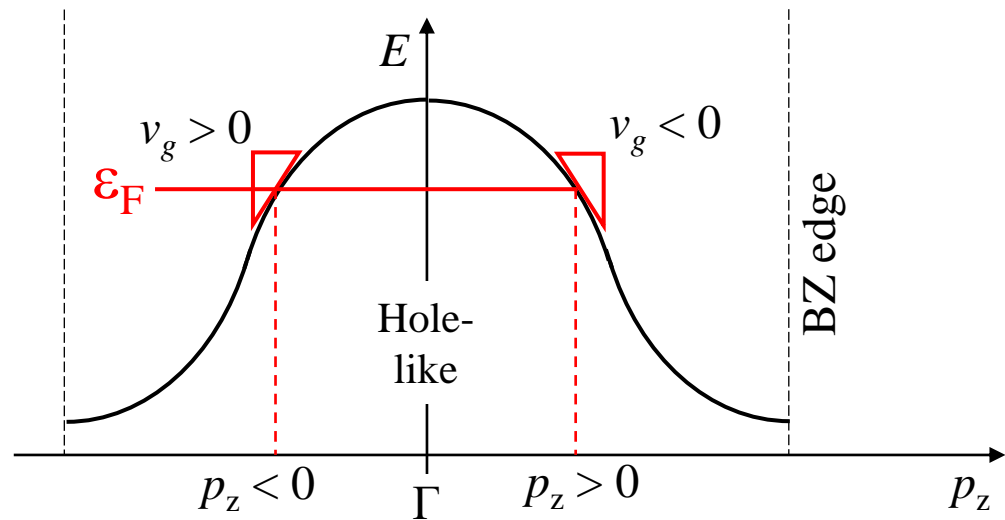
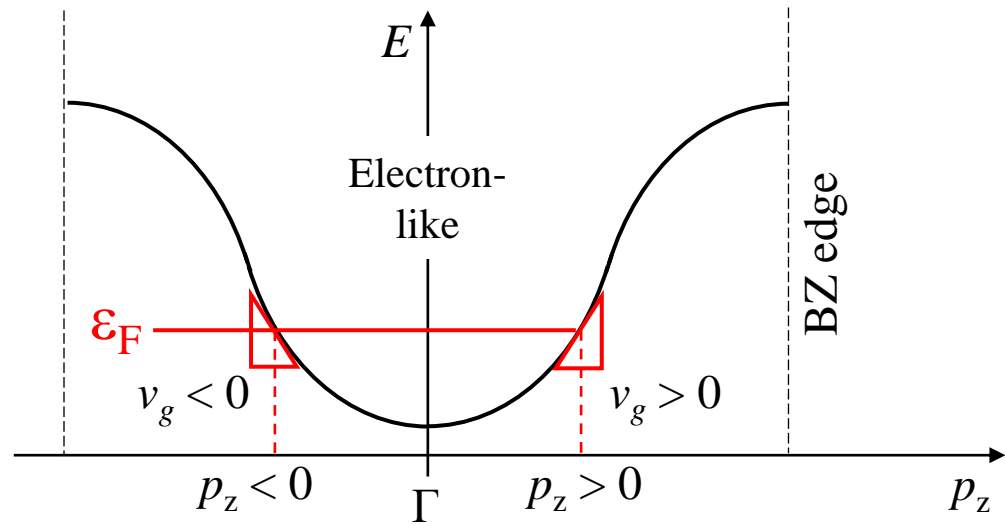
⇒ Incomplete theoretical framework

Heisenberg Uncertainty and group velocity



- Additional *required* theoretical considerations:
 - (i) Finite spatial extent of $|\psi_{excited}\rangle$ due to absorption depth, electron extraction depth, etc.
 - \Rightarrow Momentum width $\Delta p_z \geq \frac{\hbar}{2\Delta z}$
 - \therefore Convolution in \mathbf{p} -space !!
 - ... significant analytical and computational issues
 - (ii) Wave-packet nature of $|\psi_{excited}\rangle$
 - \Rightarrow Group velocity effects
 - \therefore Reduced QE for $v_g = \frac{\partial E}{\partial p_z} < 0$
 - ... positive $v_g = \frac{p}{m_0}$ for $|\psi_{vacuum}\rangle$

Group velocity effects



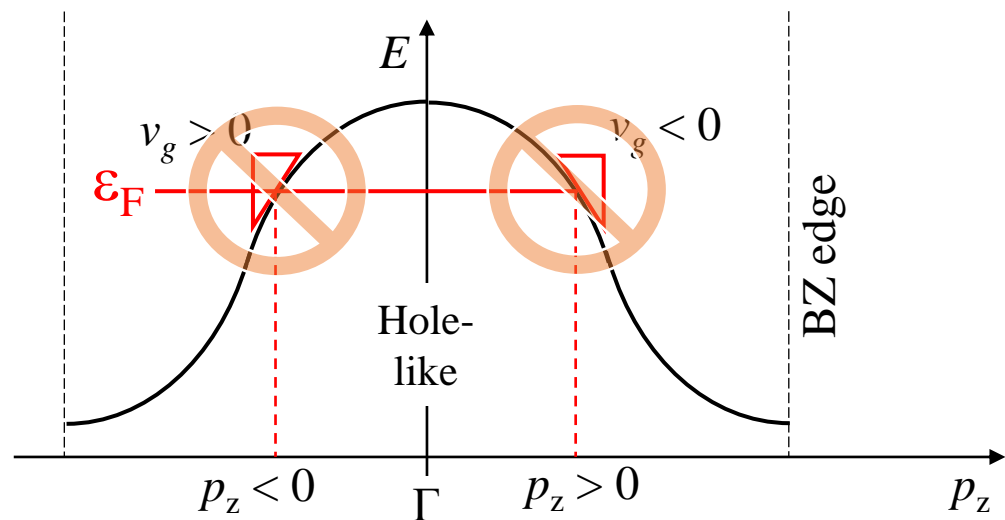
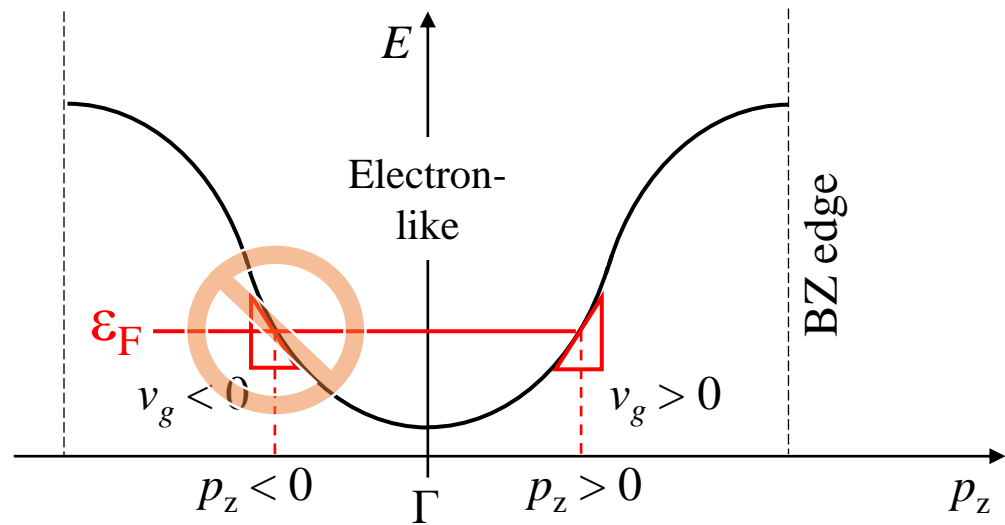
ANSATZ:

Efficient photoemission requires

(i) $p_z > 0$

(ii) $v_g = \frac{\partial E}{\partial p_z} > 0$

Group velocity effects



ANSATZ:

Efficient photoemission requires

(i) $p_z > 0$

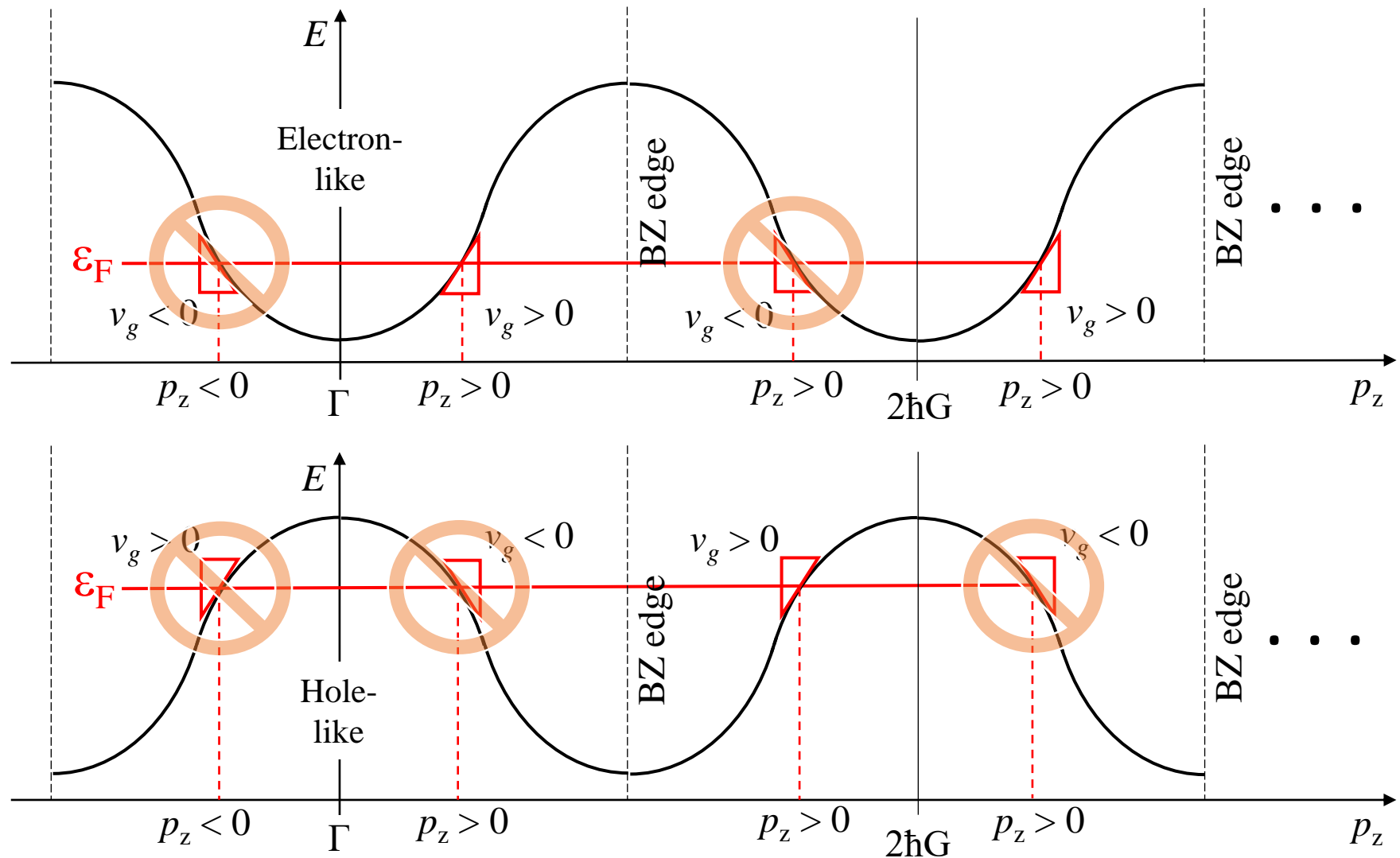
(ii) $v_g = \frac{\partial E}{\partial p_z} > 0$

\Rightarrow Only electron-like band has high QE in 1st BZ

BUT

‘Umklappen’ allows emission ...

Group velocity effects



- Hole-like band should have higher QE in 2nd BZ than in 1st BZ

PLUS

Expect contributions to QE (and hence MTE) from multiple BZs

- Direct connection of bulk band structure to spectral photoemission properties:
 - (i) GaSb(001): Excited-state thermionic emission (ESTE)
 - Measurements consistent with $MTE \geq \frac{2}{3} \left| \frac{m_T^*}{m_0} \right| \frac{m_1}{m_1+m_2} (\hbar\omega - E_g')$
 - (ii) Cu(111): Sub-threshold (non-surface-state) emission from upper conduction band
 - $E(\mathbf{p})$ of L-point bands \Rightarrow Observed spectral MTE dependence
 - (iii) Hf(0001): ‘Sub-Dowell-Schmerge’ spectral MTE dependence
 - Low m^* of hole-like emission band restricts p_T
- Further theoretical considerations:
 - (i) Heisenberg Uncertainty ...
 - (ii) Group velocity: $p_z > 0$ **and** $v_g = \frac{\partial E}{\partial p_z} > 0$ for efficient photoemission