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High quality beam generation in density downramp injection and its early applications

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10/19/2017



Outline

- Introduction
- Physics behind density downramp injection
 - Injection process
 - How this injection process leads to low emittance?
 - Transverse deceleration process
 - How this leads to low energy spread?
 - ┌ low slice energy spread – break the longitudinal phase mixing
 - └ low projected energy spread - remove the initial energy chirp
 - Scaling law and X-FEL simulations
- Conclusions

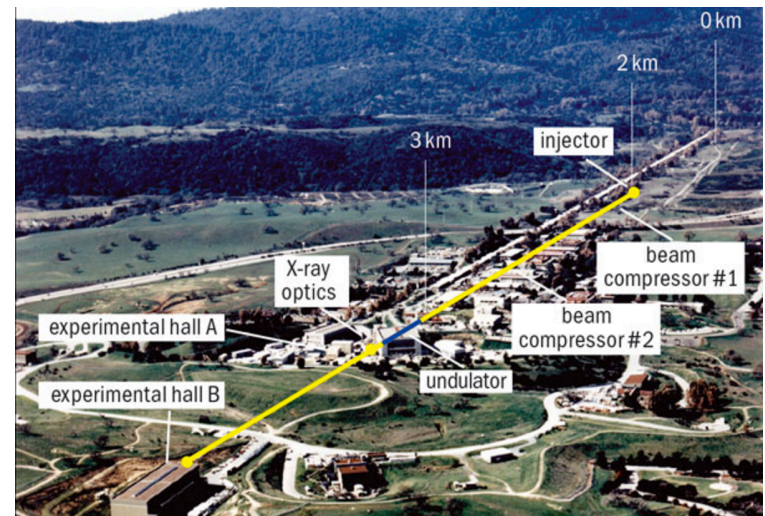
Introduction

- High quality beam generation in plasma wakefield accelerators
 - emittance
 - current
 - energy spread (slice and projected)
- } 5D Brightness $B = \frac{2I}{\epsilon_{n,x}\epsilon_{n,y}}$

X-FEL at LCLS¹:

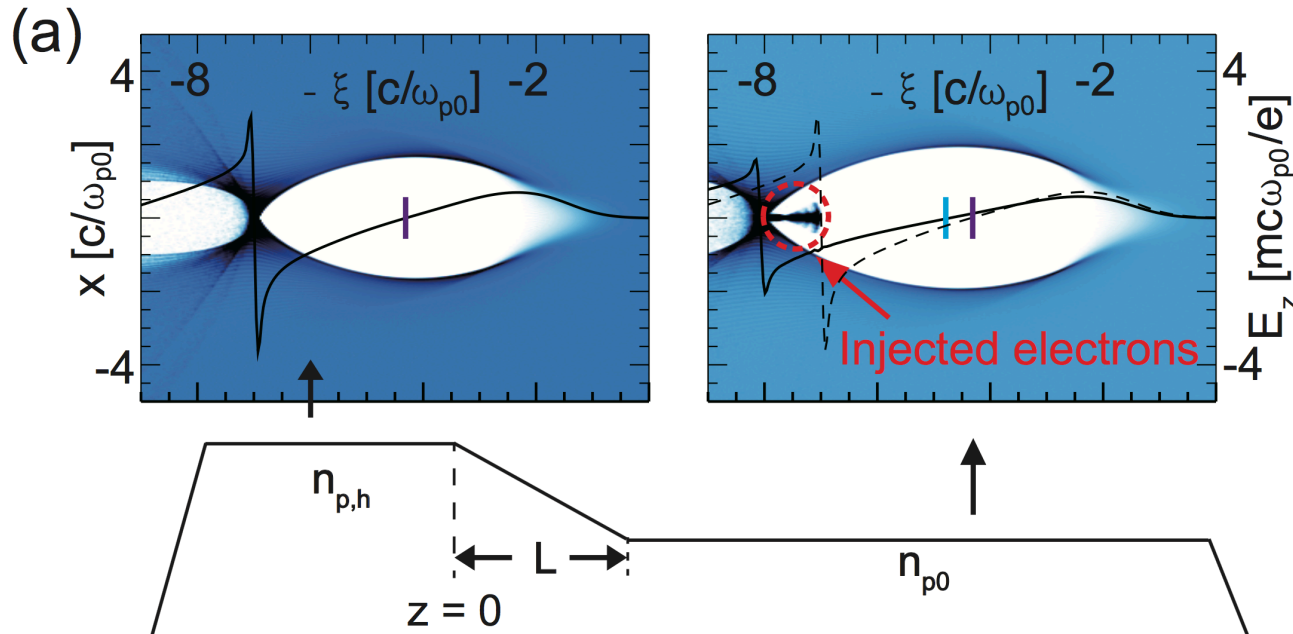
$$\sim 0.4 \times 10^{17} \text{ A/m}^2/\text{rad}^2$$

$$\sigma_\gamma/\gamma < \rho \sim 0.001$$



¹P. Emma et al., Nature Photonics 4, 641-647 (2010).

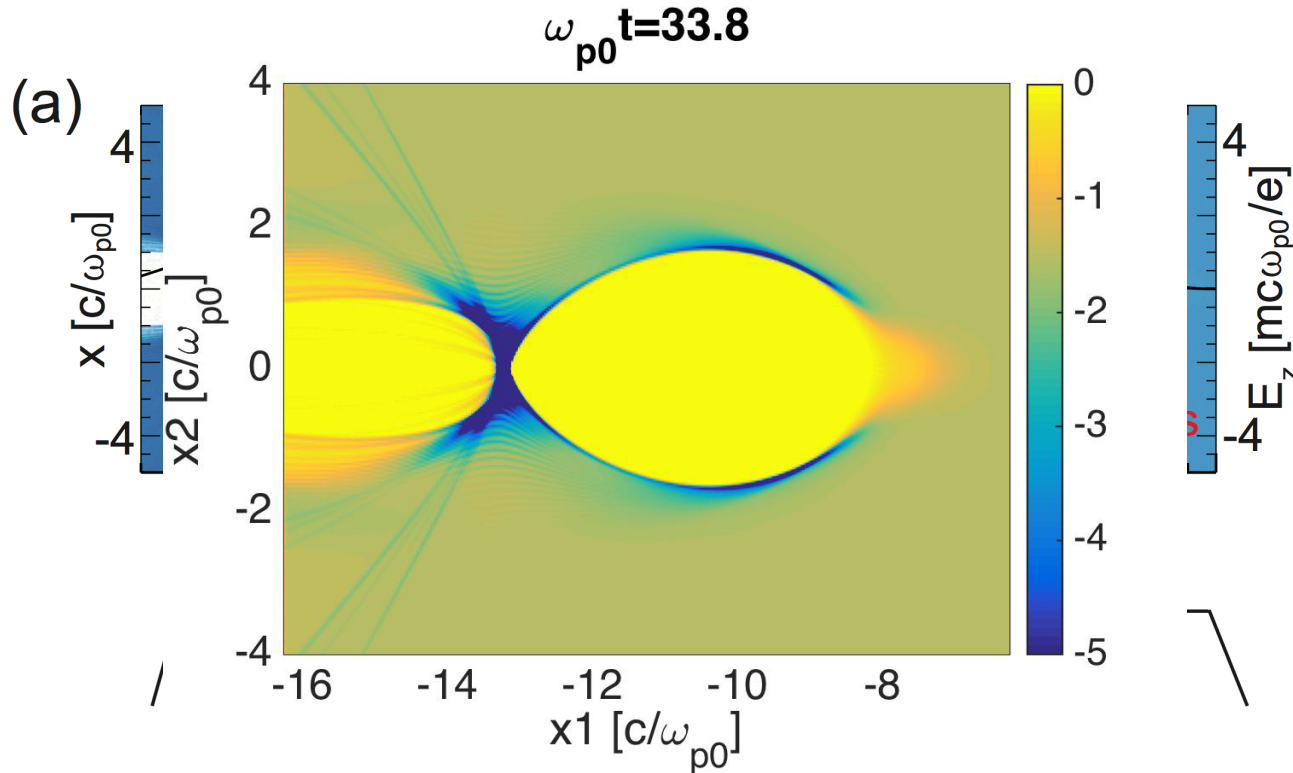
Introduction – Downramp Injection



- S. Bulanov² et al. (1998), and H. Suk³ et al. (2001) studied the injection process using **1D** analysis.

¹T. Katsouleas, Phys. Rev. A 33, 2056 (1986); ²S. Bulanov, et al., Phys. Rev. E 58, R5257 (1998); ³H. Suk, et al., Phys. Rev. Lett. 86, 1011 (2001);

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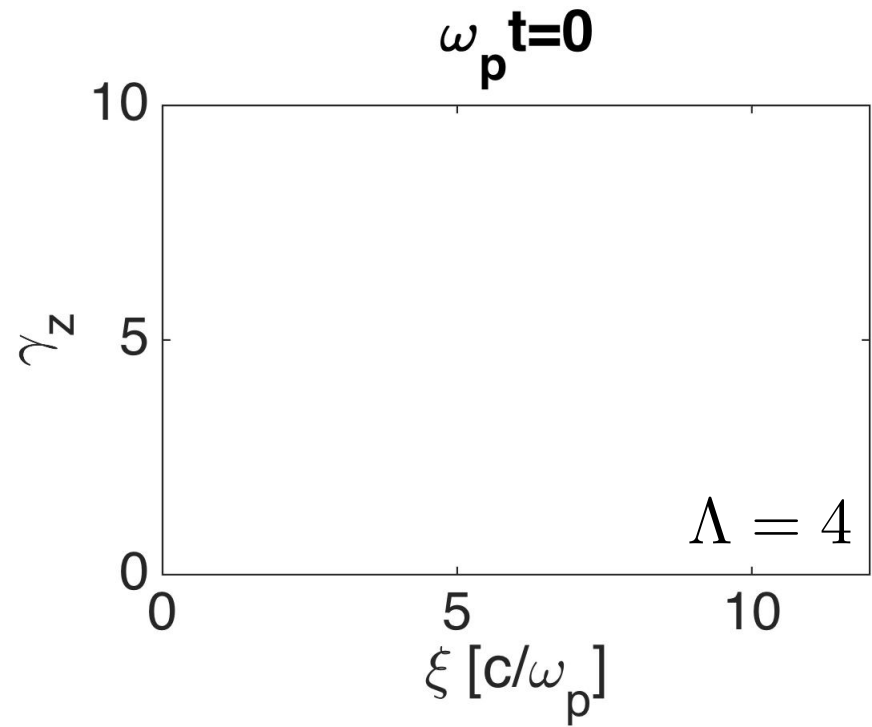
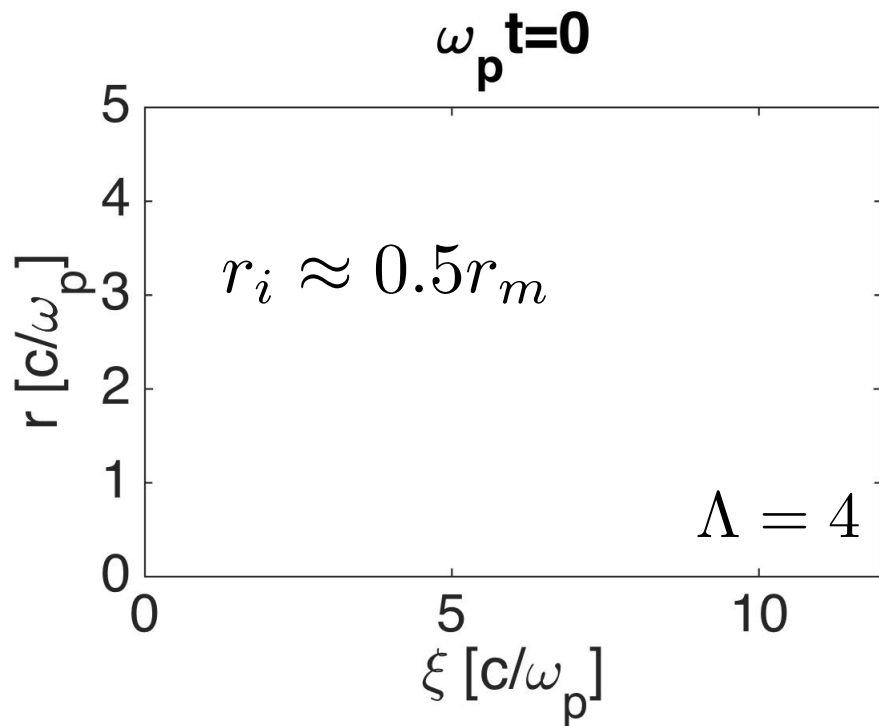
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The particle velocity β_z

Injection Condition: $\beta_z \geq \beta_{ph}$



The particle velocity β_z

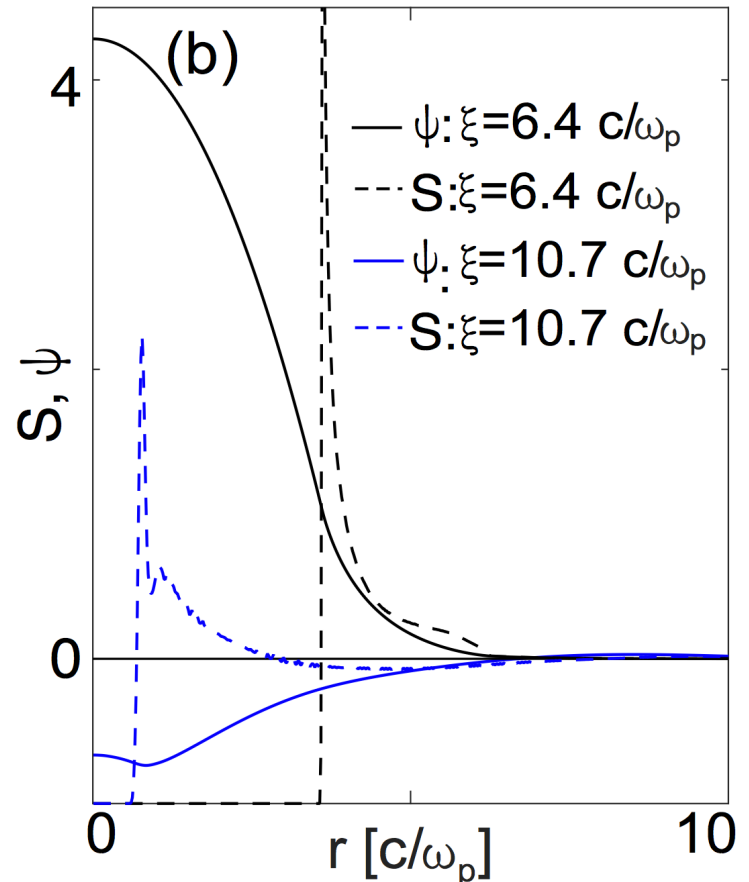
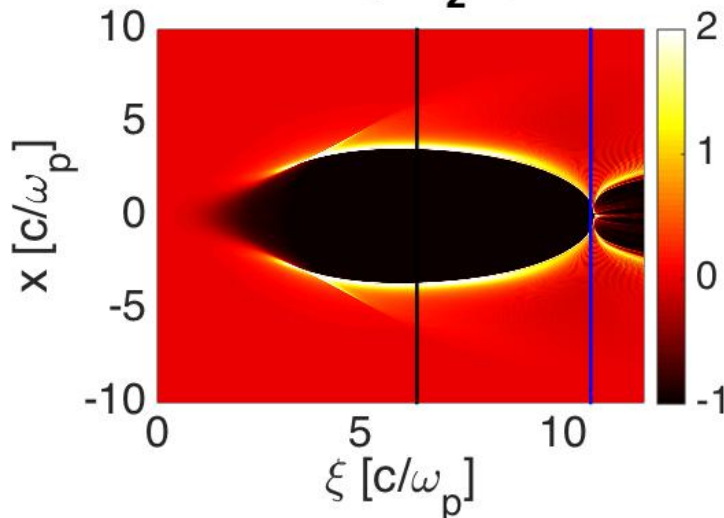
$$\beta_z = 1 - \frac{2(1 + \psi)}{1 + p_{\perp}^2 + (1 + \psi)^2}$$

large p_{\perp}
or ψ is close to -1

The Poisson-like Equation

$$\nabla_{\perp}^2 \psi = S \equiv -(\rho - J_z/c)$$

$$S = -(\rho - J_z/c)$$

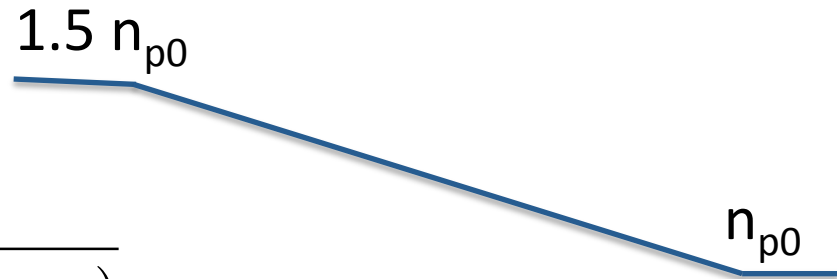


The phase velocity β_{ph}

- For a plasma wake

$$\phi(z, t) = \omega_p(z)(z/v_d - t)$$

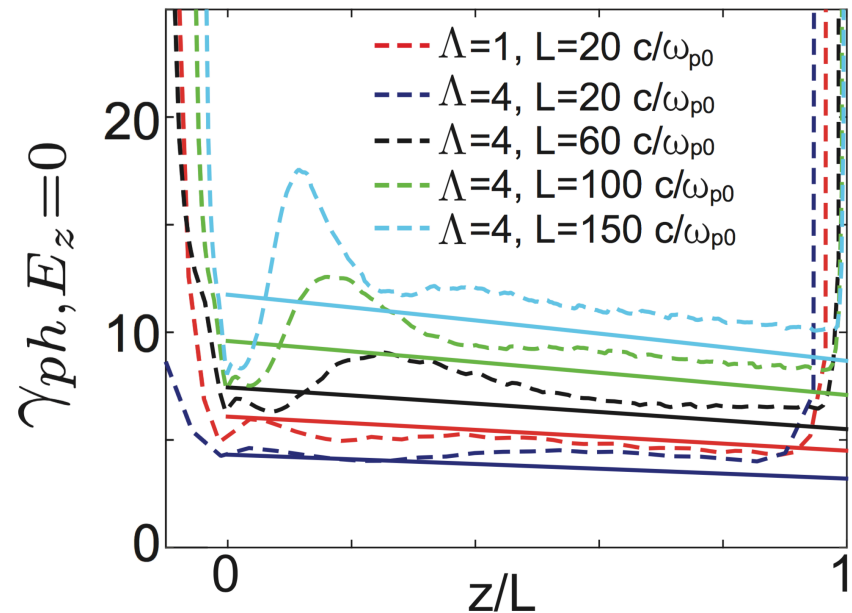
$$v_{ph}(z, t) = \frac{v_d}{1 - (d\omega_p/dz)\omega_p^{-1}(v_d t - z)}$$



For the tail of the nonlinear wake¹,

$$v_{ph} \approx v_d \left(1 - 4\sqrt{\Lambda} \frac{d\omega_p^{-1}}{dz} \right)$$

$$\gamma_\phi \approx \left(8\sqrt{\Lambda} \frac{d\omega_p^{-1}}{dz} \right)^{-1/2}$$



¹W. Lu et al., PRL 96, 165002 (2006)

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Transverse Deceleration

- The transverse force on the “sheath” plasma electrons

$$F_r = F_d + F_i + F_e$$

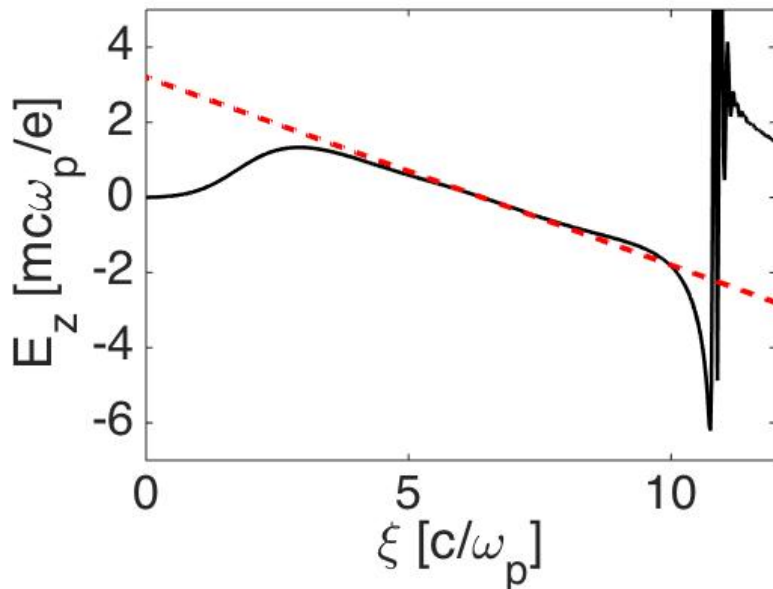
where $F_d = (1 - \beta_z)\lambda(\xi)/r$ is from the driver

----- **D**

$F_i = -r/2$ is from the ion cavity

----- **F**

$F_e = -(r/2)(1 - \beta_z)dE_z/d\xi$ is from the plasma electrons. -- **D**



In most of the wake,

$$\frac{d^2\psi_0}{d\xi^2} = \frac{dE_z}{d\xi} = -\frac{1}{2}$$

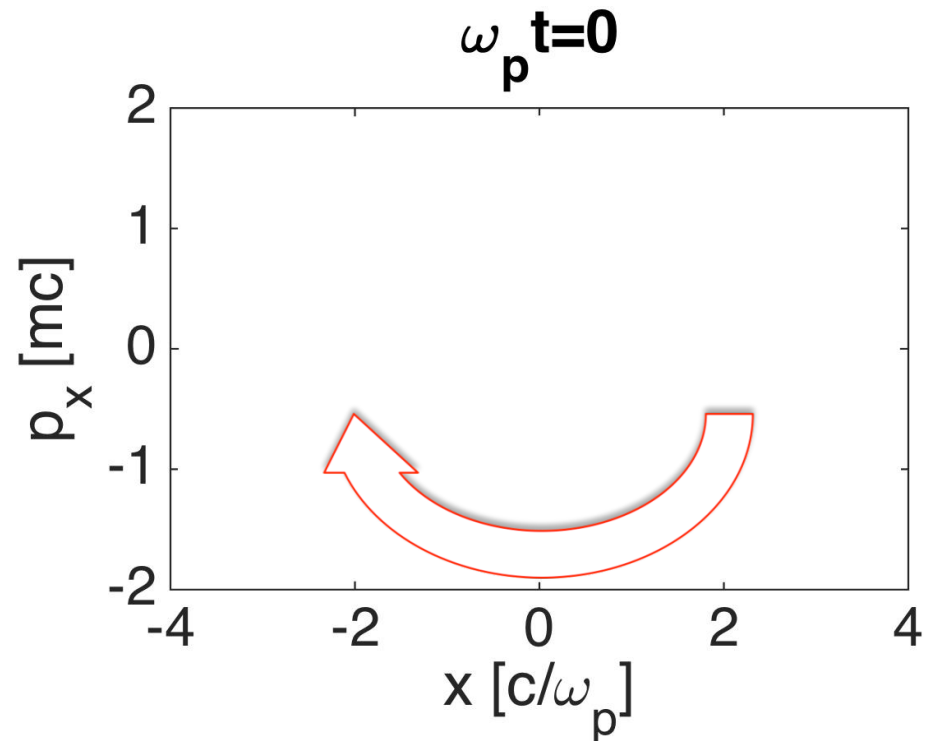
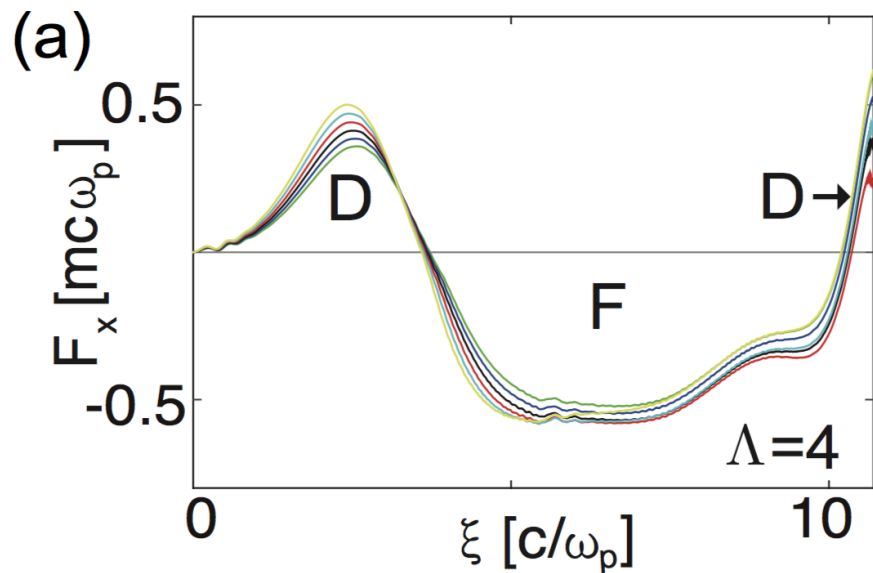
At the very rear of the wake,

$$\left| \frac{d^2\psi_0}{d\xi^2} \right| \gg 1$$

Transverse Deceleration

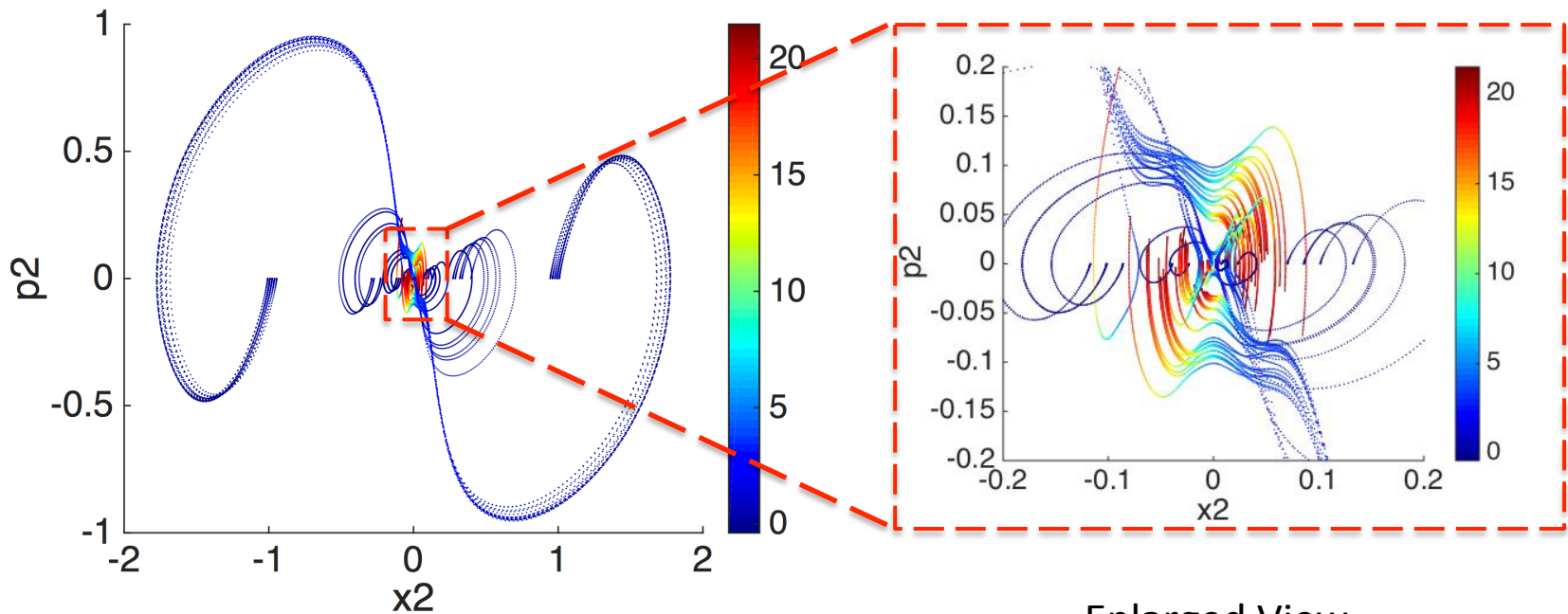
- The transverse force on the “sheath” plasma electrons

$$F_r = F_d + F_i + F_e$$



High brightness beam generation

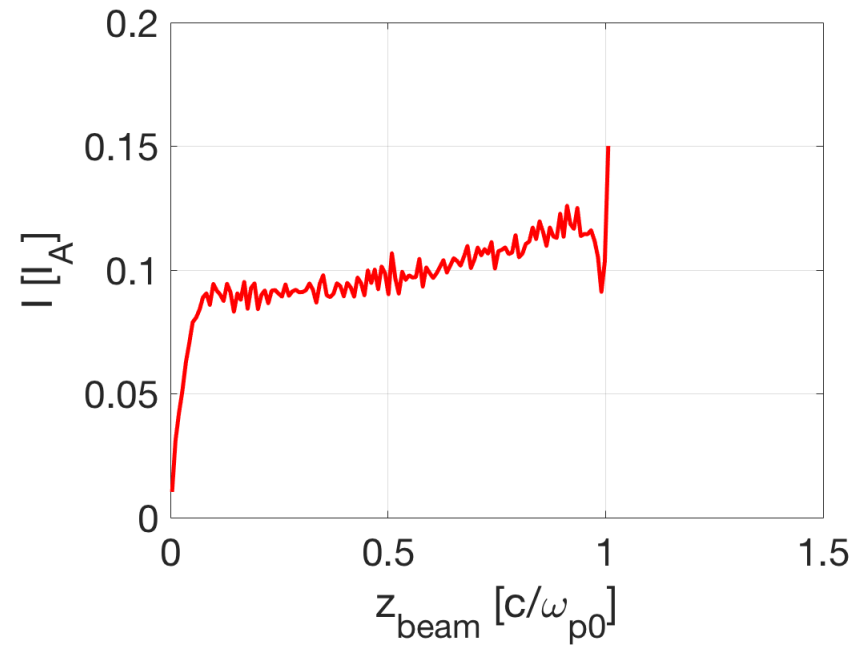
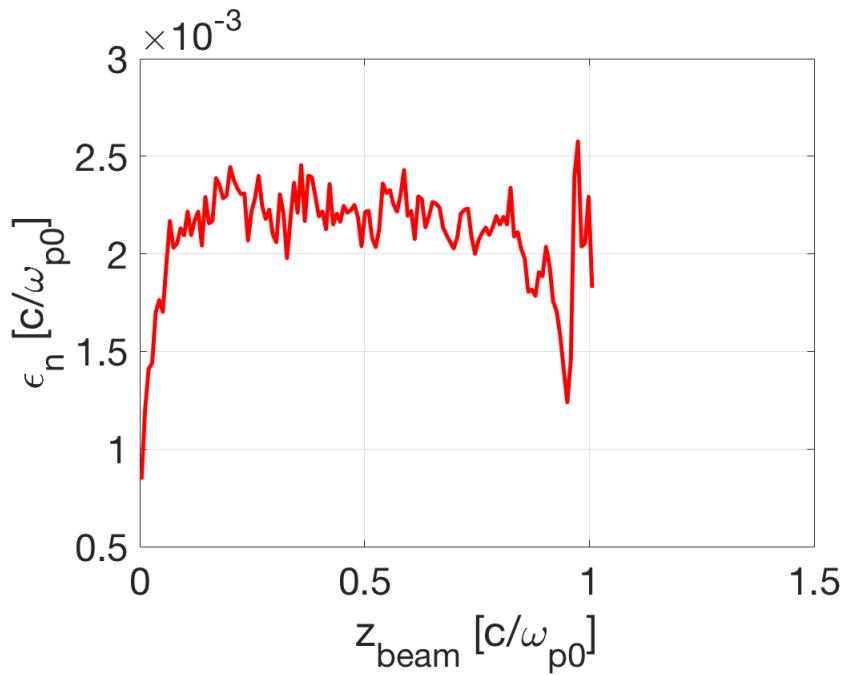
The trajectories of the injected electrons in downramp injection:



$$\Lambda = 1, n_{p,h} = 1.5n_{p0}, L = 20c/\omega_{p0}$$

Enlarged View

High brightness beam generation

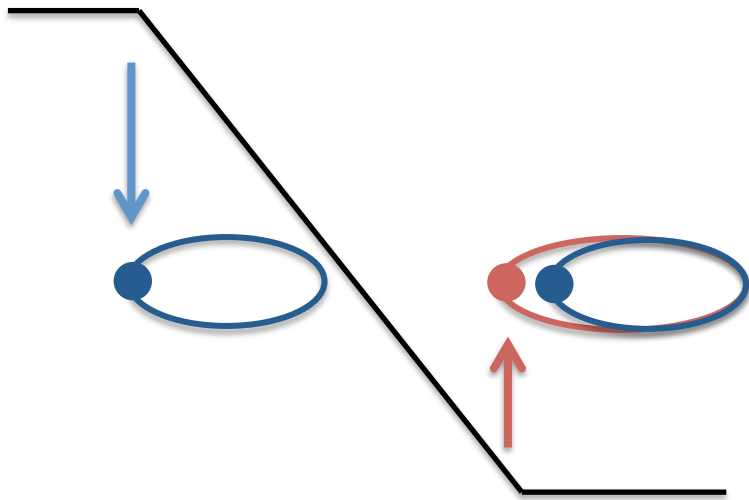


$$\Lambda=1, n_{p,h}=1.5 n_{p0}, L=20 c/\omega_{p0}$$

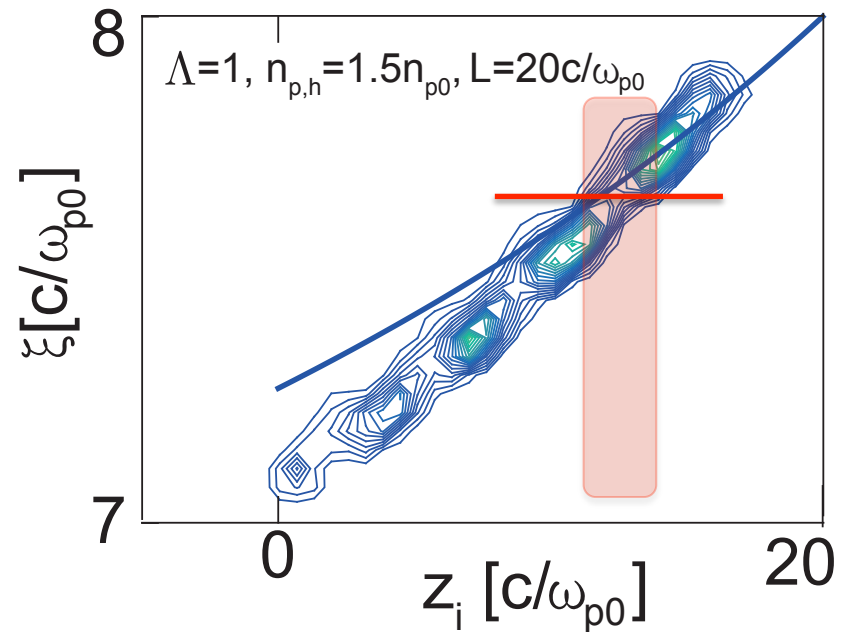
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Low slice energy spread - Relations between z_i and ξ_f



$$\frac{d\xi}{dz_i} \approx \frac{d\lambda_{wake}}{dz_i} \approx 2 \frac{dr_m}{dz_i}$$

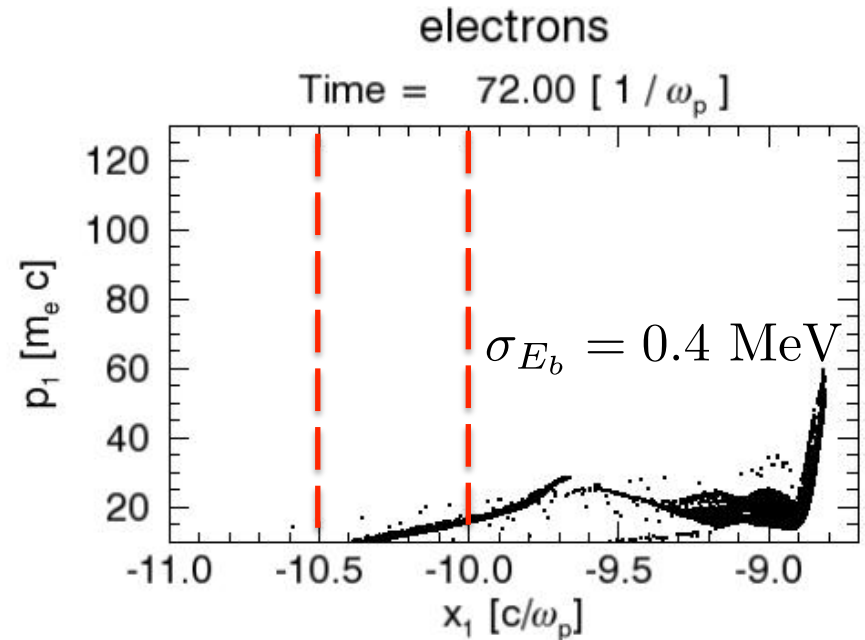
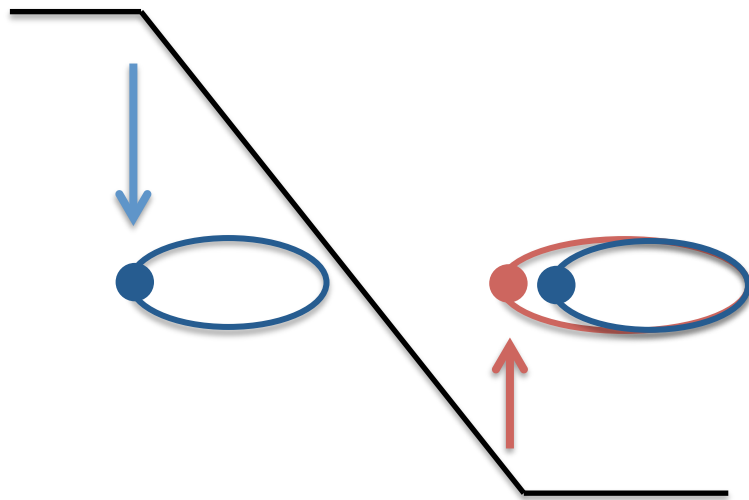


Longitudinal phase mixing¹ is broken!

Slice energy spread $\sim O(0.1)$ MeV!

¹X. L. Xu, et al., PRL 112, 035003 (2014).

Low projected energy spread – play with the chirp

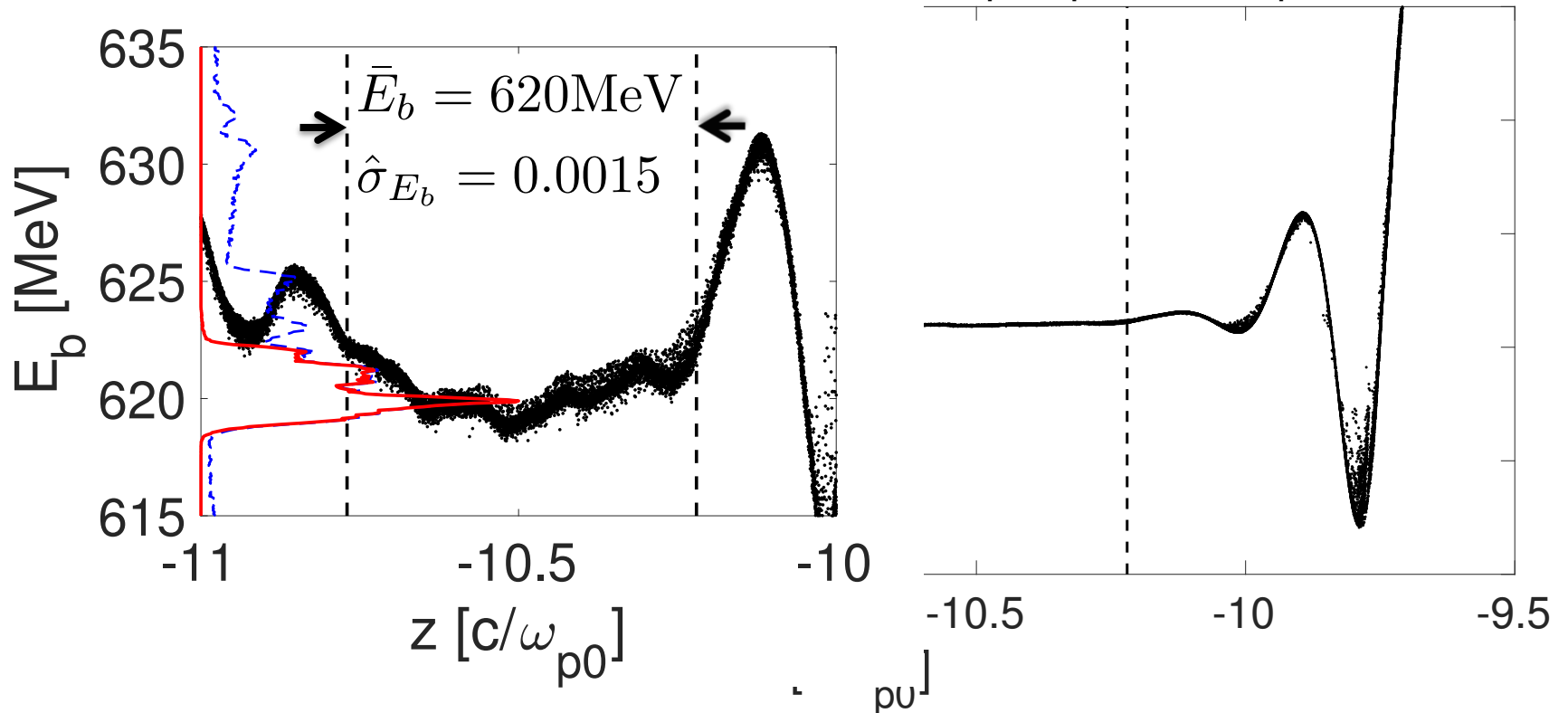


Initial energy chirp $\Delta\gamma_i = -\kappa\Delta\xi_i$ can be removed when $L_{acc} = 2\kappa$ and $\gamma_o = \gamma_i + \kappa\xi_i$ at this optimized distance.

Low projected energy spread – play with the chirp

$$\gamma_o = \gamma_i + \boxed{\kappa} \xi_i$$

Evolving Driver: $\Lambda=4$, $\sigma_z = \sigma_r = c/\omega_{p0}$, $\epsilon_n = c/\omega_{p0}$, $1.5 n_{p0} \rightarrow n_{p0}$ ($L=250 c/\omega_{p0}$), $T_e=10$ eV



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Scaling law

	I	ϵ_n, τ and σ_r	B	σ_E/E	n	Q
e ⁻ Beams	n_{p0}^0	$n_{p0}^{-0.5}$	n_{p0}^1	n_{p0}^0	n_{p0}^1	$n_{p0}^{-0.5}$
	Ramp Length ¹			Acceleration Distance ²		
Plasma	$\propto n_{p0}^{-0.5}$			$\propto n_{p0}^{-0.5}$		

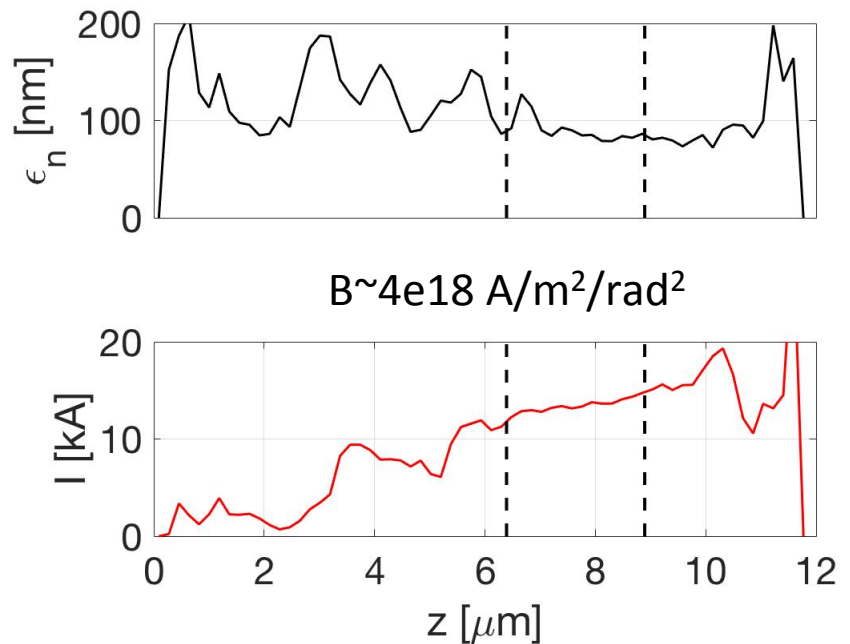
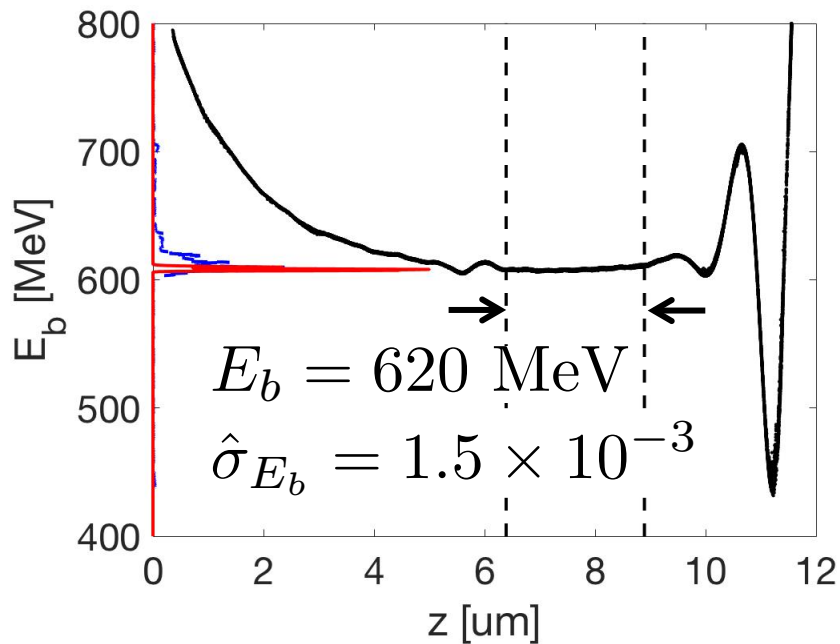
Take $1.5 n_{p0} \rightarrow n_{p0}$ ($L=250 c/\omega_{p0}$) as an example:

	n_{p0} [cm ⁻³]	I [kA]	ϵ_n [nm]	τ [fs]	σ_r [um]	B [A/m ² / rad ²]	E [MeV]	σ_E/E	Q [pC]
Injected beam	10^{18}	14	80	10	0.2	4e18	620	1.5e-3	140
	10^{20}	14	8	1	0.02	4e20	620	1.5e-3	14
	n_{p0} [cm ⁻³]	Density change [cm ⁻³]		L_{ramp} [mm]	L_{acc} [mm]				
Plasma	10^{18}	0.5e18		1.33	3.3				
	10^{20}	0.5e20		0.133	0.33				

¹For fixed density change; ²To remove the energy chirp.

Injector for an X-FEL

	I [kA]	σ_r [um]	σ_z [um]	ϵ_n [um]	Q [nC]	E_b [GeV]
Driver beam	34 ($\Lambda=4$)	5.3	5.3	5.3	1.5	10
	$n_{p,h}$ [cm ⁻³]	n_{p0} [cm ⁻³]	L_{ramp} [mm]	L_{acc} [mm]	Initial T [eV]	
Plasma	1.5e18	1e18	1.33 (250 c/ω_{p0})	3.3	10	



X-FELs Driven by Plasma Accelerators

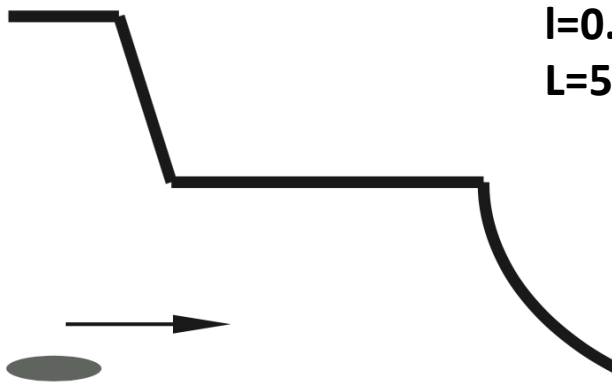
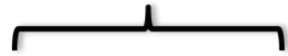
High quality beam generation



Matching
Plasma Matching + Quadrupoles

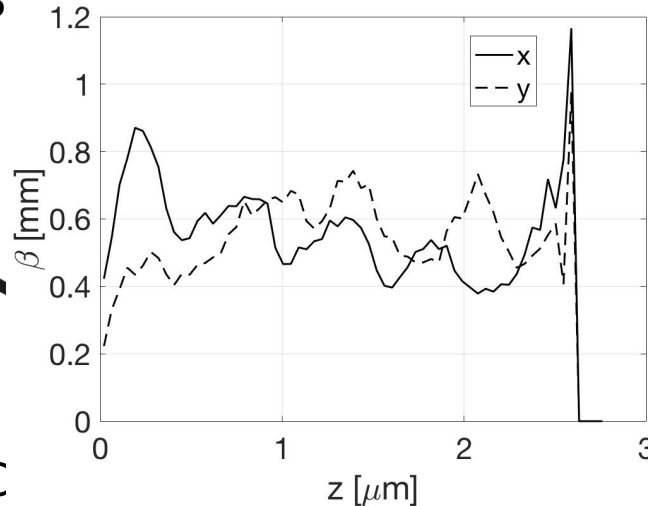


Radiator

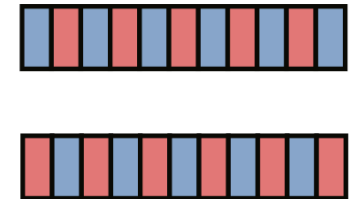


$l=0.30\text{mm}$
 $L=5$

4 quads, $\sim 300\text{ T/m}$



Codes: OSIRIS (+ QuickPIC

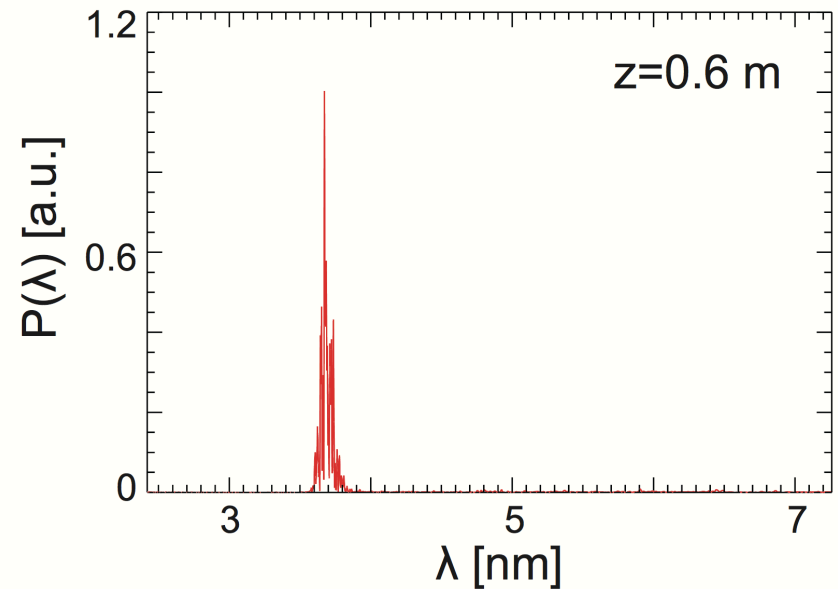
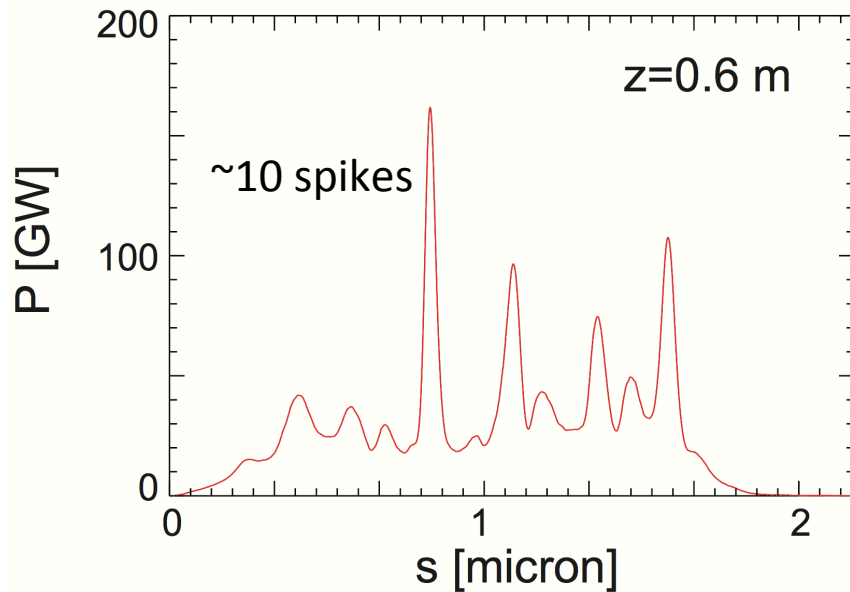


Genesis 1.3

FEL radiation – soft X-ray

- Undulator: $\lambda_u=0.5$ cm, $K=1^1 \rightarrow \lambda_r=3.6$ nm

Genesis 1.3 Simulation Results¹:



¹S. Reiche, Nucl. Instrum. Methods Phys. Res., Sect. A 429, 243 (1999).

Conclusions

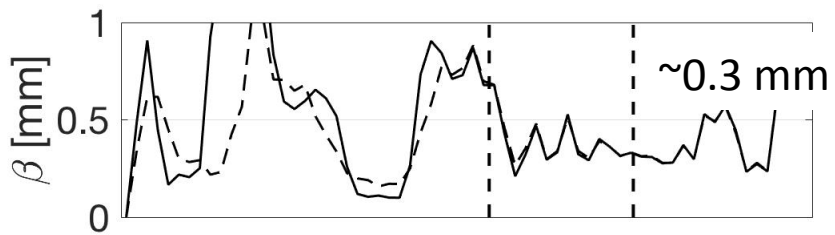
- We studied the injection dynamics in downramp injection in the 3D blowout regime and found high quality (high current, low emittance, low slice and projected energy spread) electron beams can be generated with suitable parameters.
- By combining the plasma matching section and quadrupoles, this high quality beam can be transported to the undulator to drive a X-FEL.

- Thanks!

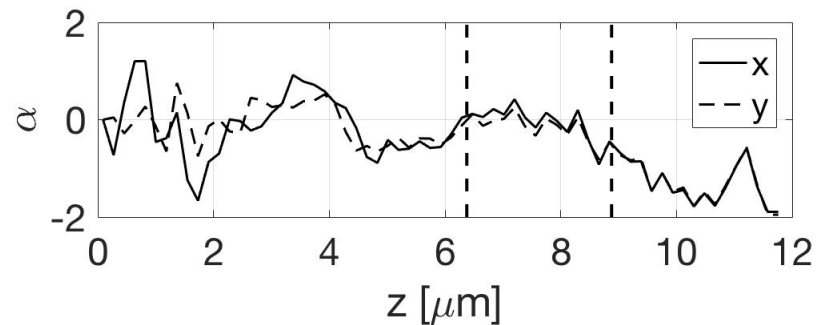
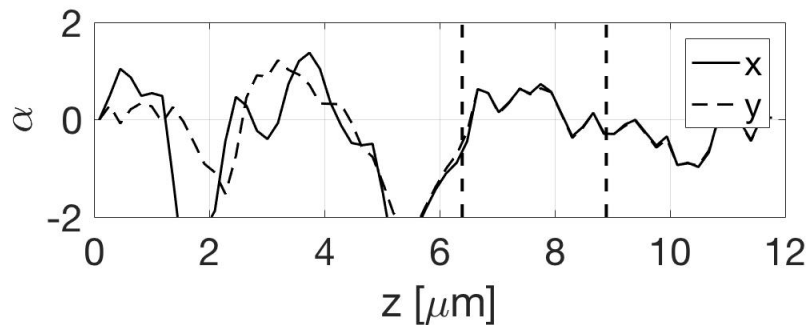
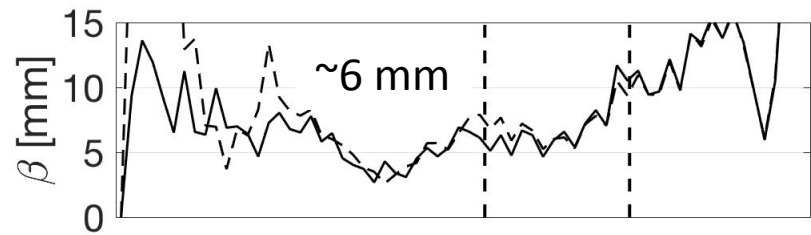
Plasma Matching Section

- Characteristic $l=0.30$ mm, Total $L=5.7$ mm

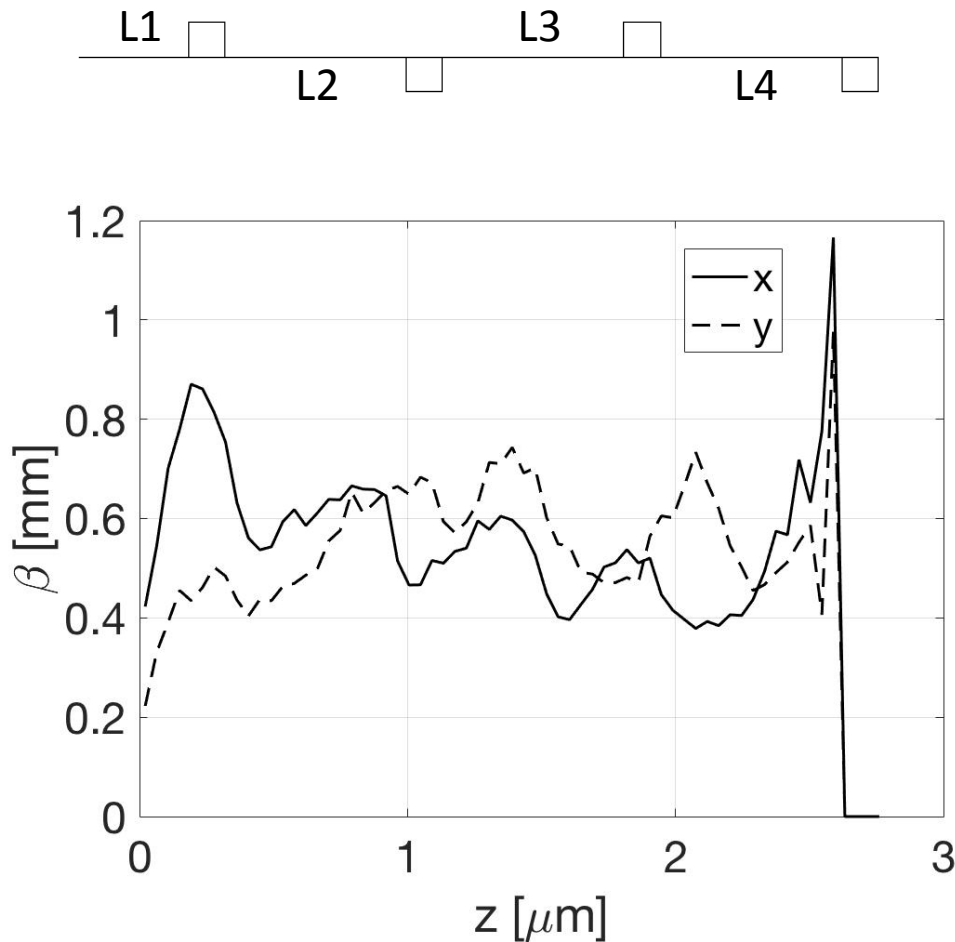
Before Matching section



After Matching section



Magnetic transport lines



Parameters	Value
L1 [m]	0.3
L2 [m]	0.9
L3 [m]	0.9
L4 [m]	0.9
K1 [m ⁻²]	28.1
K2 [m ⁻²]	-16.3
K3 [m ⁻²]	16.4
K4 [m ⁻²]	134.9*
Width [m]	0.1

*corresponding to 270 T/m